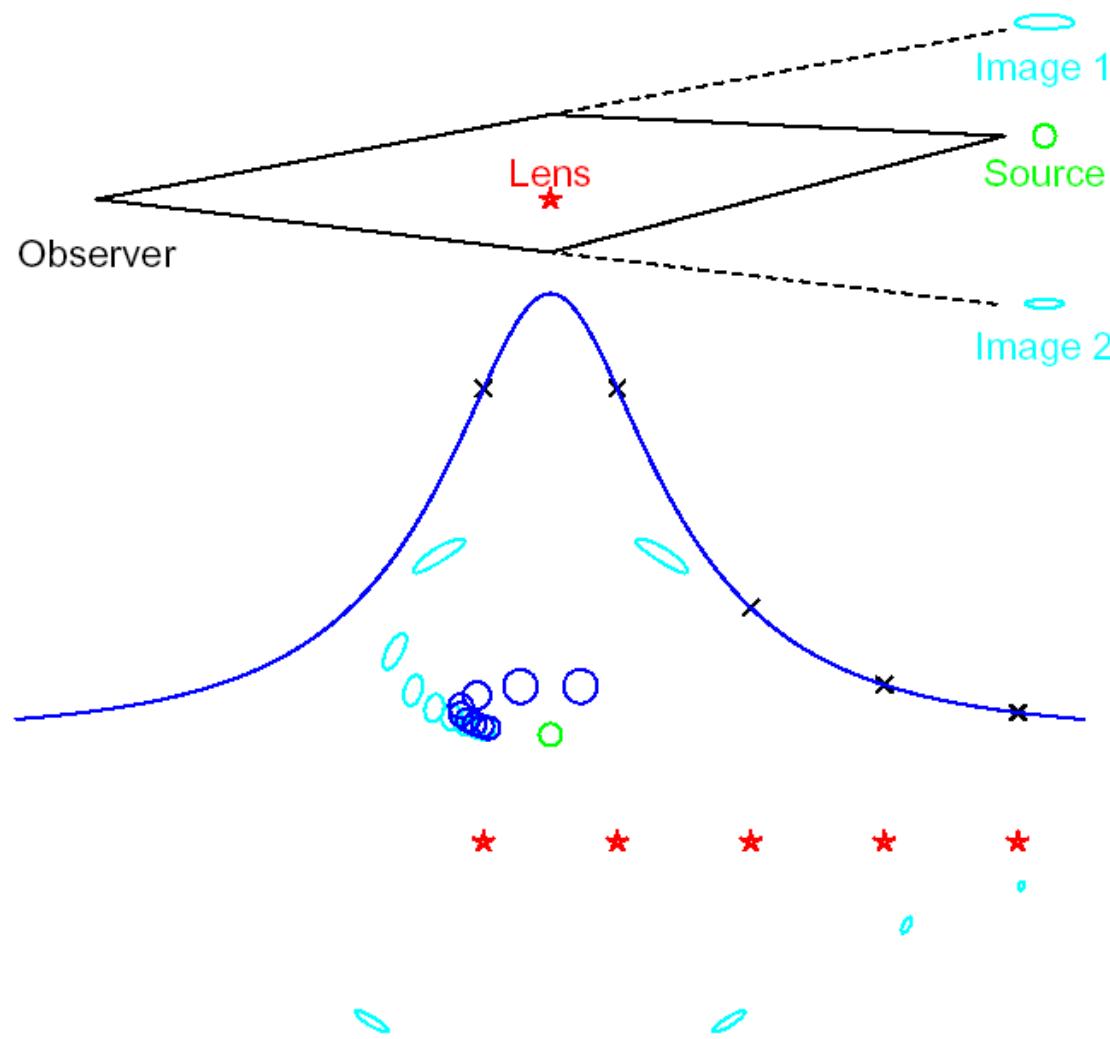


# Microlensing VII: Applications to Astrophysics

## Andy Gould (Ohio State)



# Variable Stars

- Deep connection to microlensing

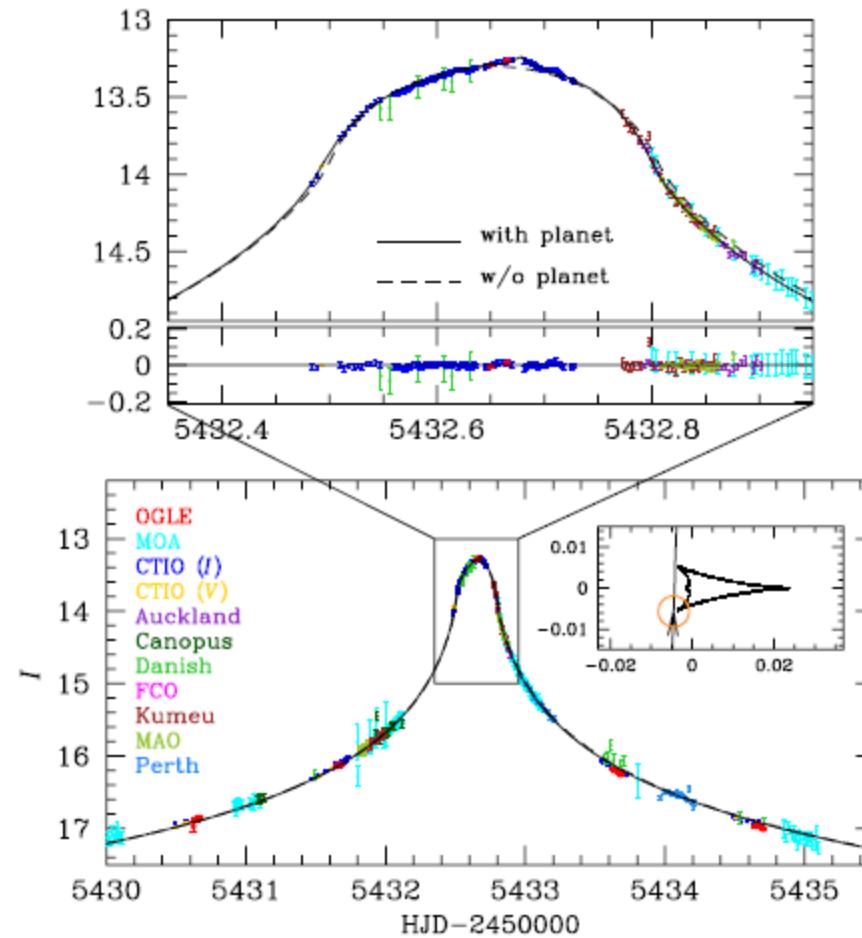
# Variable Stars

- Deep connection to microlensing
  - Many thought: insurmountable contaminant

# Variable Stars

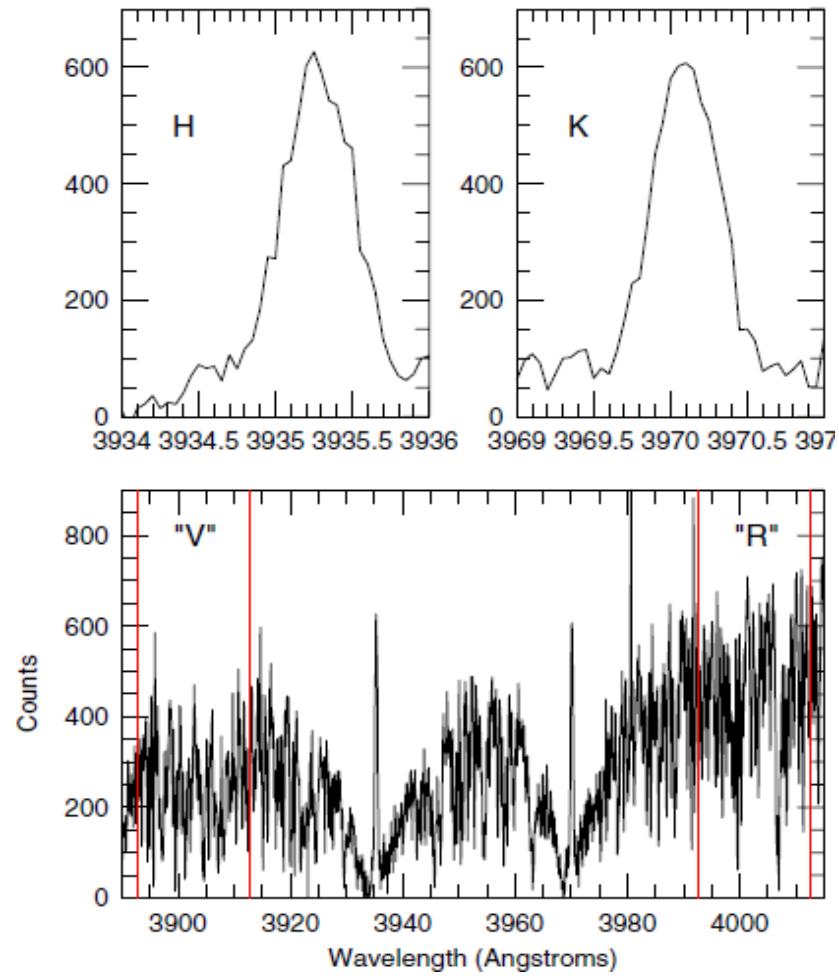
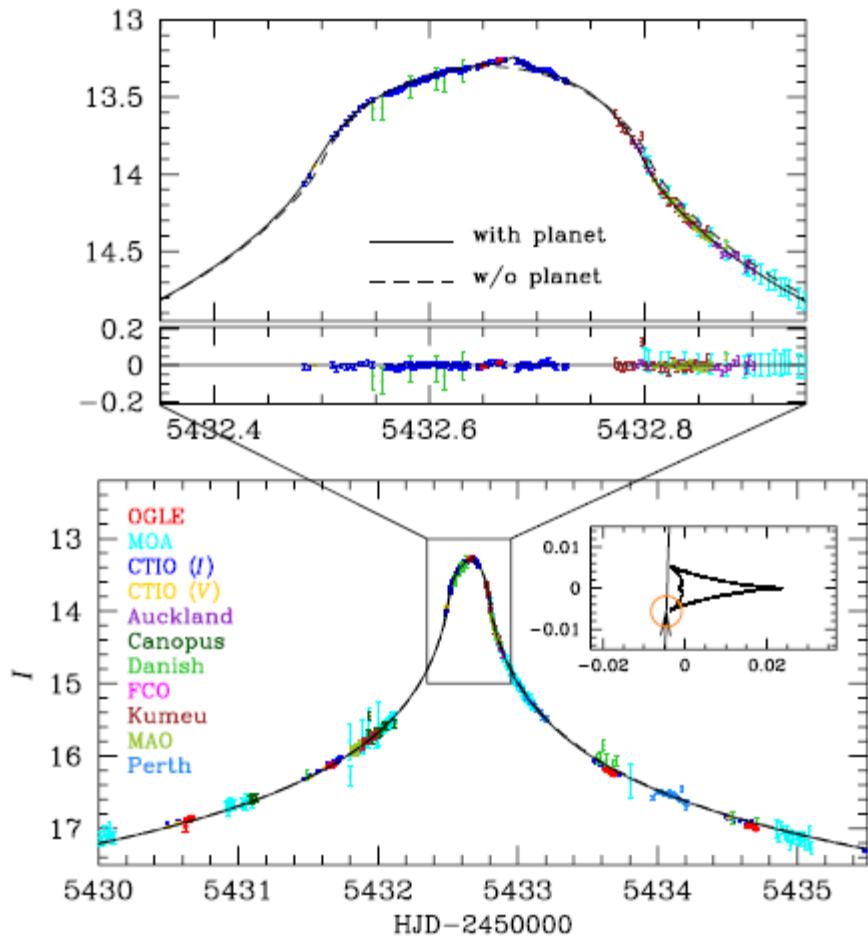
- Deep connection to microlensing
  - Many thought: insurmountable contaminant

# MOA-2010-BLG-523: “Failed” Planet



Gould, Yee, et al. 2013, ApJ, 763, 141

# MOA-2010-BLG-523: “Failed” Planet



Gould, Yee, et al. 2013, ApJ, 763, 141

# Variable Stars

- Deep connection to microlensing
  - Many thought: insurmountable contaminant
  - Main driver for Polish OGLE survey

P. PIETRUKOWICZ<sup>1</sup>, A. UDALSKI<sup>1</sup>, I. SOSZYŃSKI<sup>1</sup>, D. M. NATAF<sup>2</sup>, Ł. WYRZYKOWSKI<sup>1,3</sup>, R. POLESKI<sup>1</sup>, S. KOZŁOWSKI<sup>1</sup>,  
M. K. SZYMAŃSKI<sup>1</sup>, M. KUBIAK<sup>1</sup>, G. PIETRZYŃSKI<sup>1,4</sup>, AND K. ULACZYK<sup>1</sup>

<sup>1</sup> Warsaw University Observatory, Al. Ujazdowskie 4, 00-478 Warszawa, Poland

<sup>2</sup> Department of Astronomy, Ohio State University, 140 West 18th Avenue, Columbus, OH 43210, USA

# Variable Stars

- Deep connection to microlensing
  - Many thought: insurmountable contaminant
  - Main driver for Polish OGLE survey
- RR Lyrae Stars

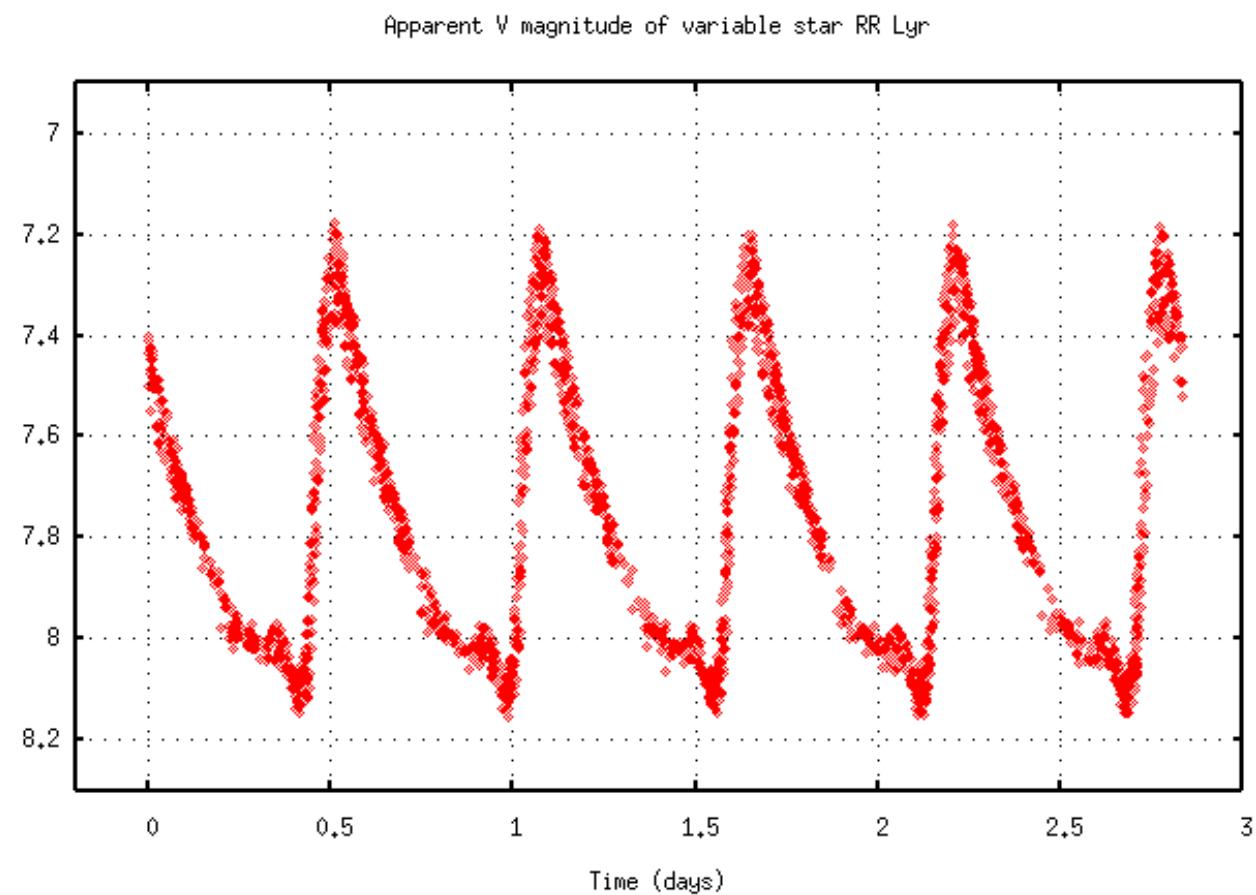
THE OPTICAL GRAVITATIONAL LENSING EXPERIMENT: ANALYSIS OF THE BULGE RR LYRAE POPULATION FROM THE OGLE-III DATA

P. PIETRUKOWICZ<sup>1</sup>, A. UDALSKI<sup>1</sup>, I. SOSZYŃSKI<sup>1</sup>, D. M. NATAF<sup>2</sup>, Ł. WYRZYKOWSKI<sup>1,3</sup>, R. POLESKI<sup>1</sup>, S. KOZŁOWSKI<sup>1</sup>,  
M. K. SZYMAŃSKI<sup>1</sup>, M. KUBIAK<sup>1</sup>, G. PIETRZYŃSKI<sup>1,4</sup>, AND K. ULACZYK<sup>1</sup>

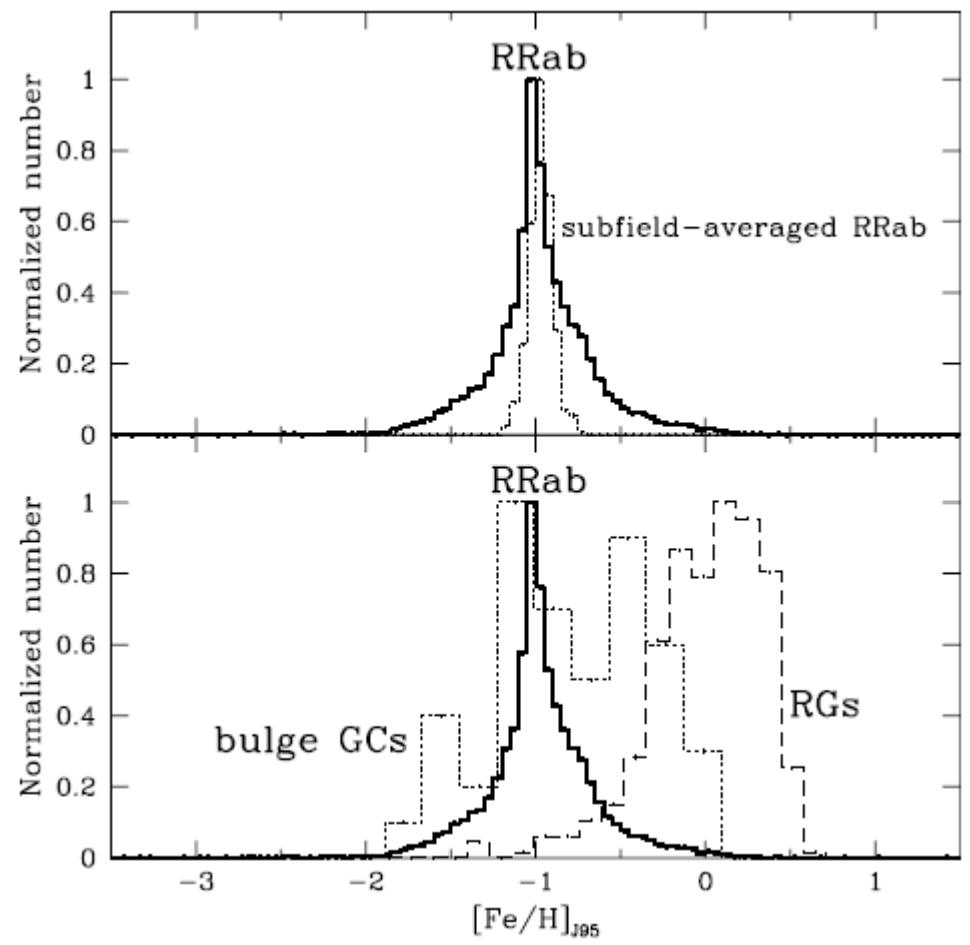
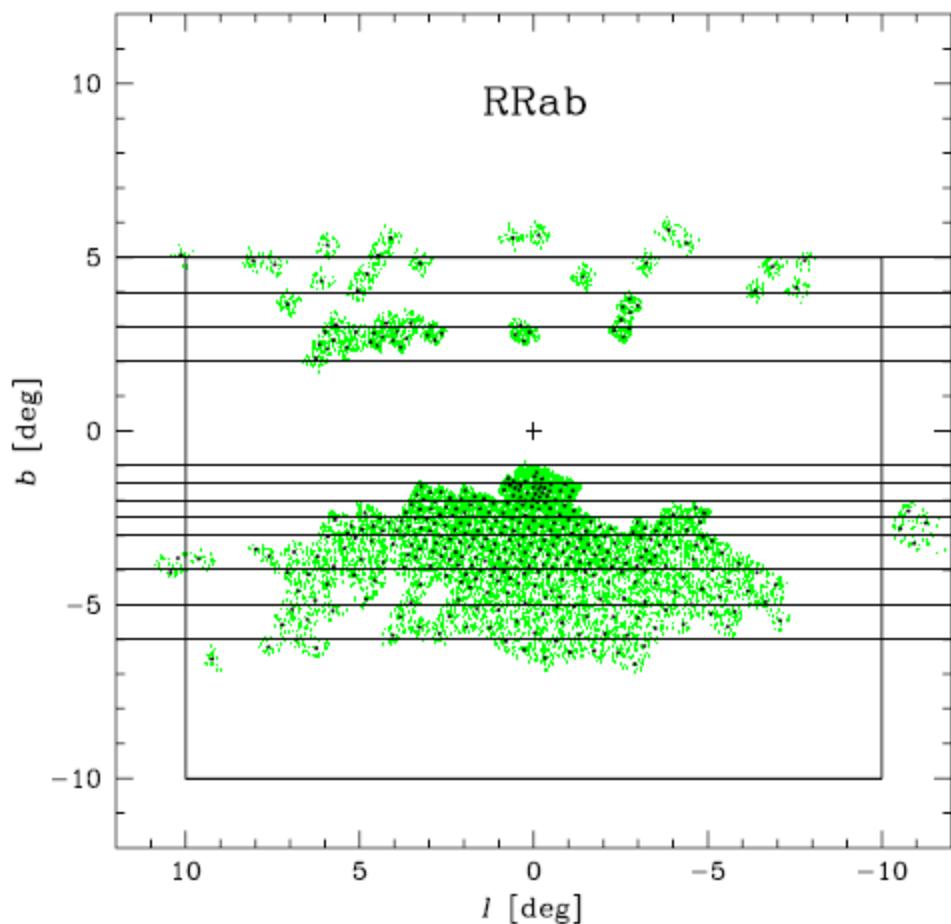
<sup>1</sup> Warsaw University Observatory, Al. Ujazdowskie 4, 00-478 Warszawa, Poland

<sup>2</sup> Department of Astronomy, Ohio State University, 140 West 18th Avenue, Columbus, OH 43210, USA

# RR Lyra

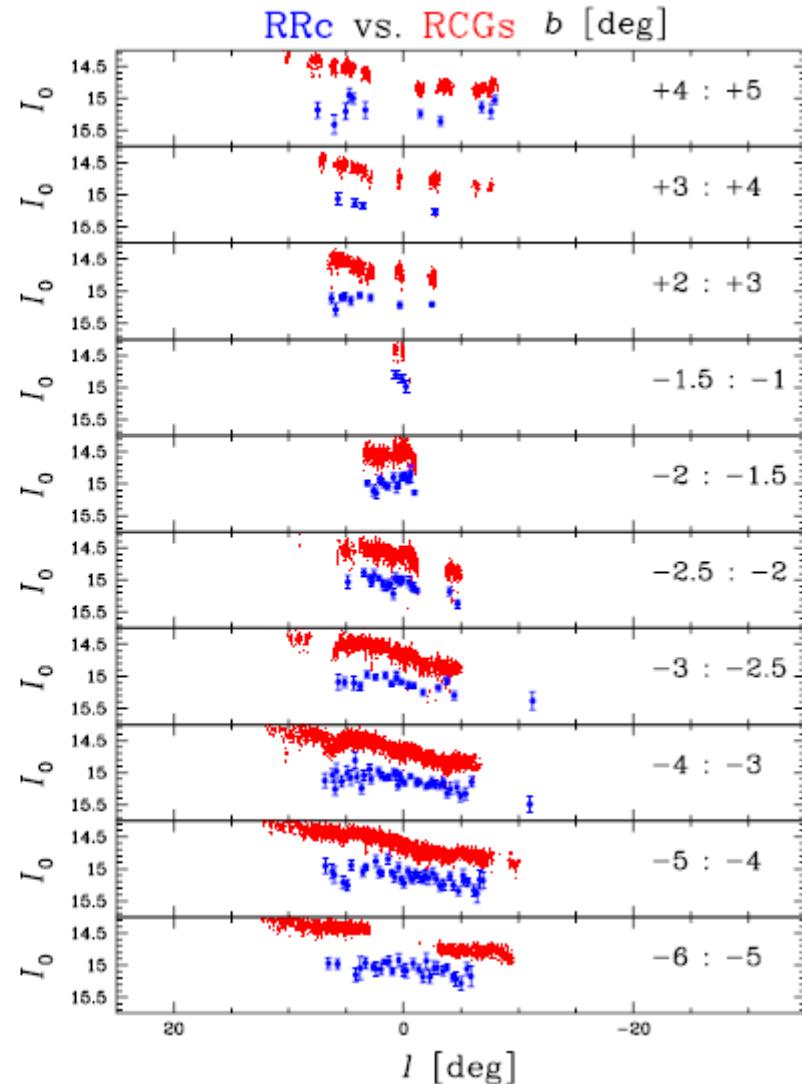
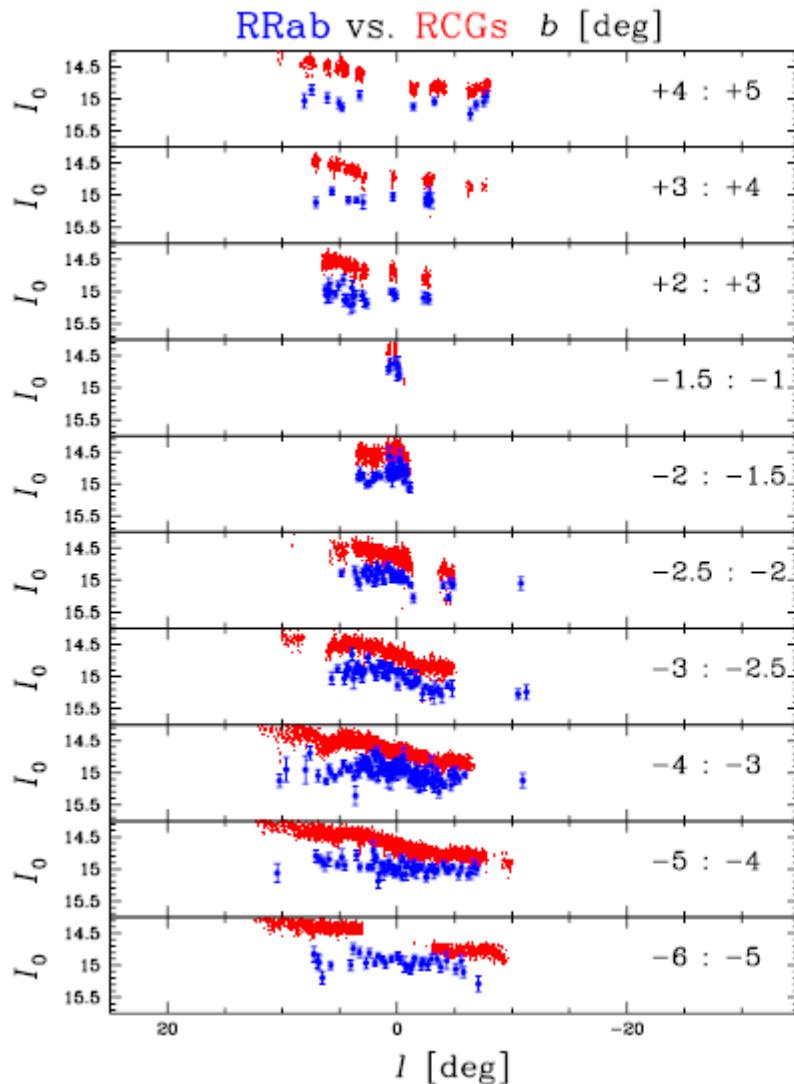


# 11,000 RR Lyrae Stars in Bulge



Pietrukowicz et al. 2012, ApJ, 750, 169

# 11,000 RR Lyrae Stars in Bulge



Pietrukowicz et al. 2012, ApJ, 750, 169

# Variable Stars

- Deep connection to microlensing
  - Many thought: insurmountable contaminant
  - Main driver for Polish OGLE survey
- RR Lyrae Stars
- Eclipsing Binaries, Delta Scutis,

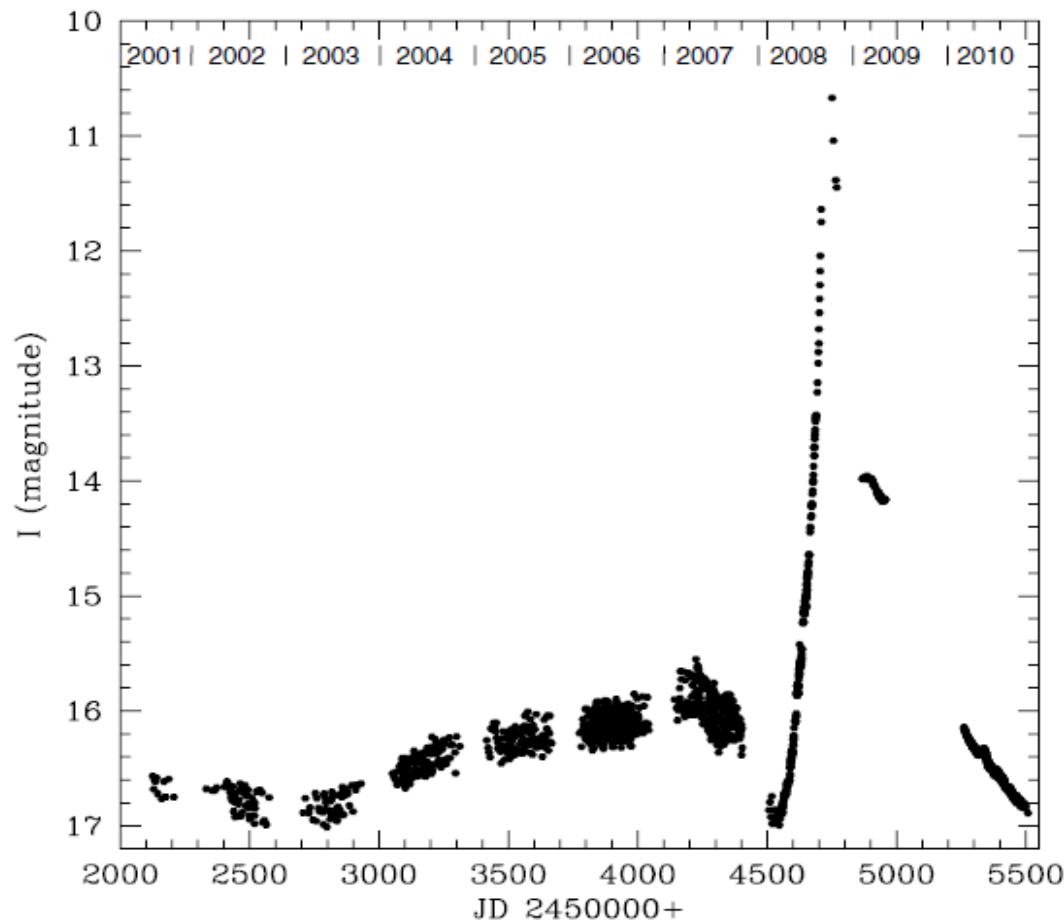
# Variable Stars

- Deep connection to microlensing
  - Many thought: insurmountable contaminant
  - Main driver for Polish OGLE survey
- RR Lyrae Stars
- Eclipsing Binaries, Delta Scutis,
- Pulsating Giants, Cataclysmic Variables

# Variable Stars

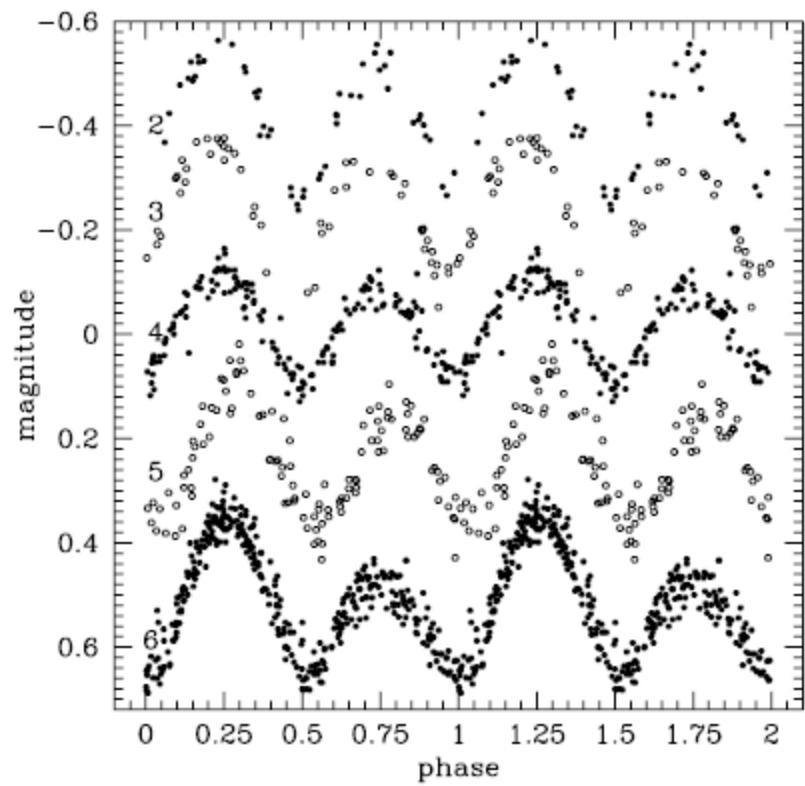
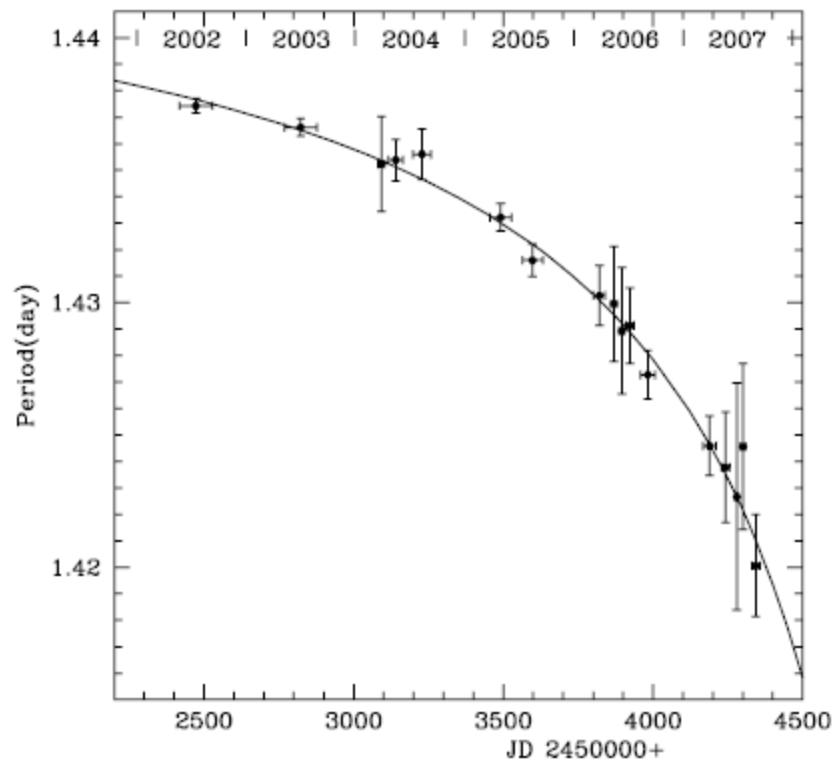
- Deep connection to microlensing
  - Many thought: insurmountable contaminant
  - Main driver for Polish OGLE survey
- RR Lyrae Stars
- Eclipsing Binaries, Delta Scutis,
- Pulsating Giants, Cataclysmic Variables
- Novae, .... and much more

# Variable Stars: Rare Merging Binaries



Tylenda et al. 2011, A&A, 528, 114

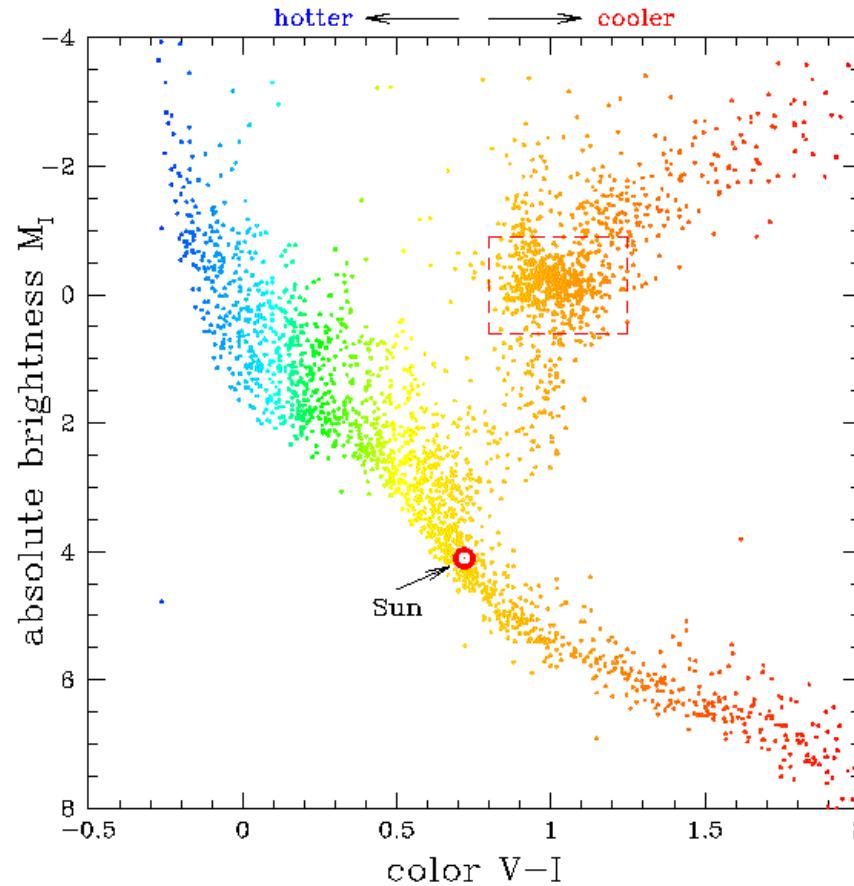
# Variable Stars: Rare Merging Binaries



Tylenda et al. 2011, A&A, 528, 114

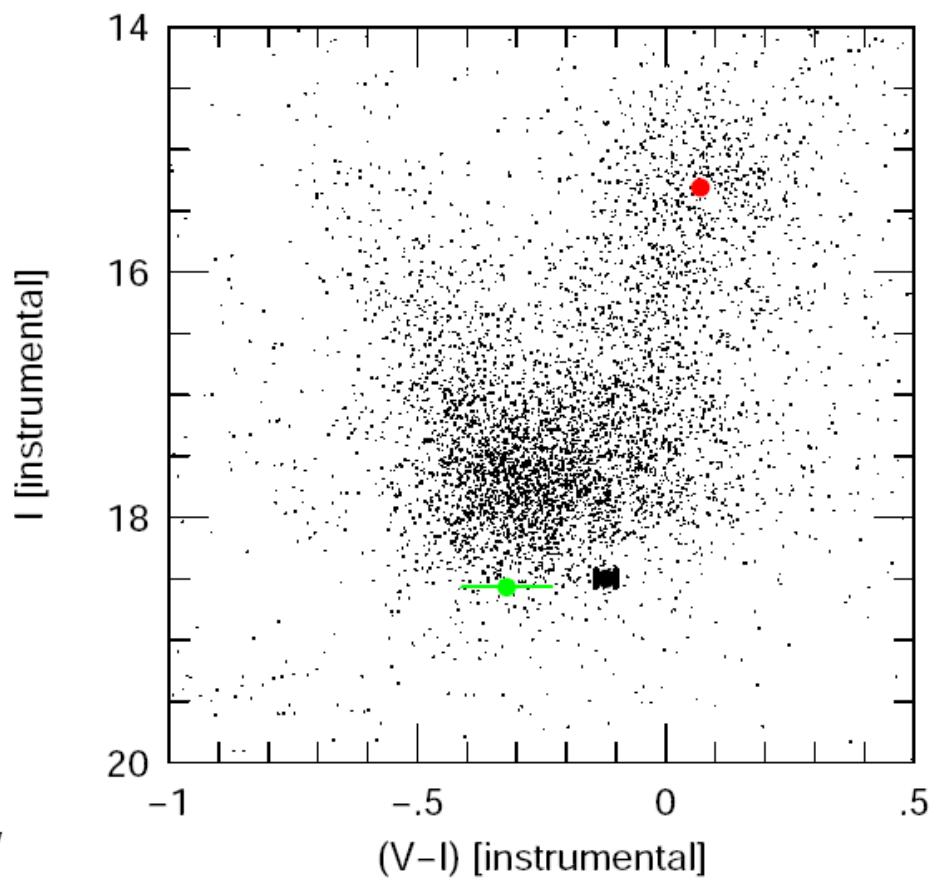
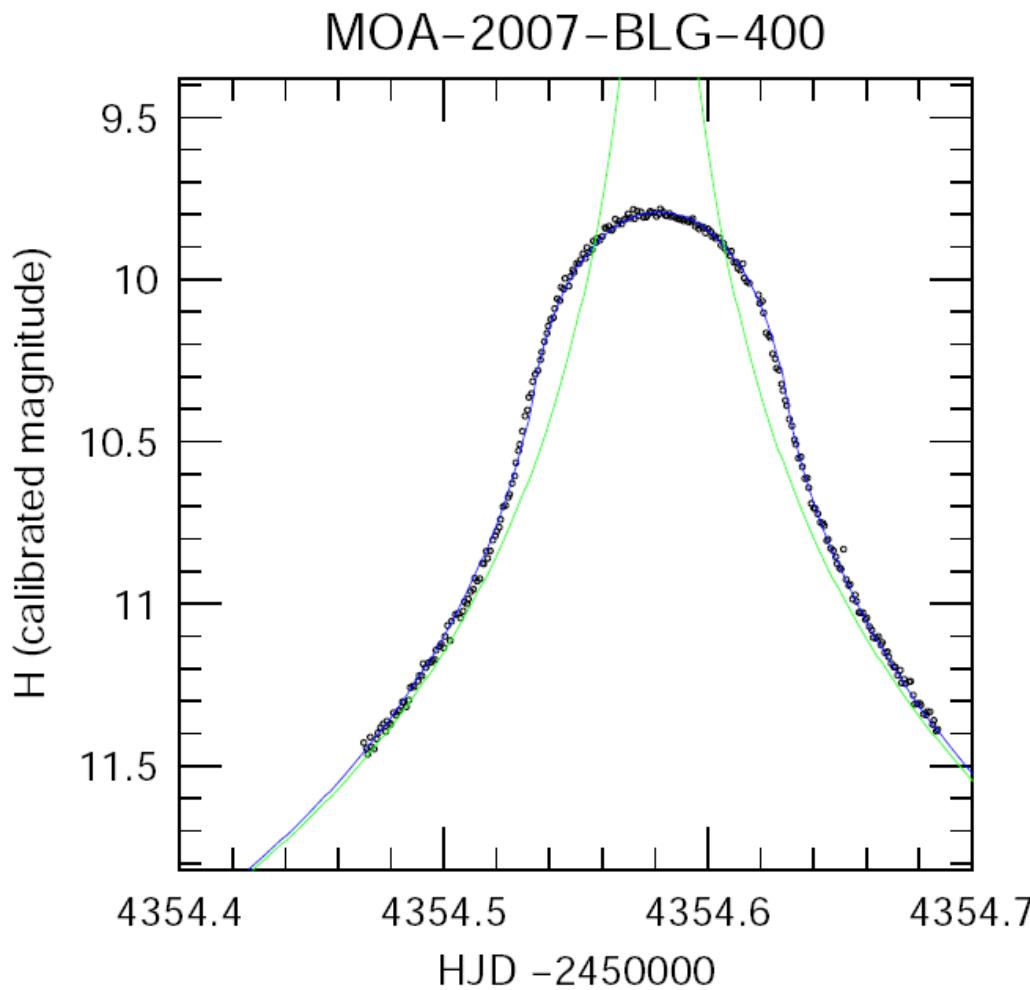
# Galactic Structure and Dust

## (mainly from Red Clump)

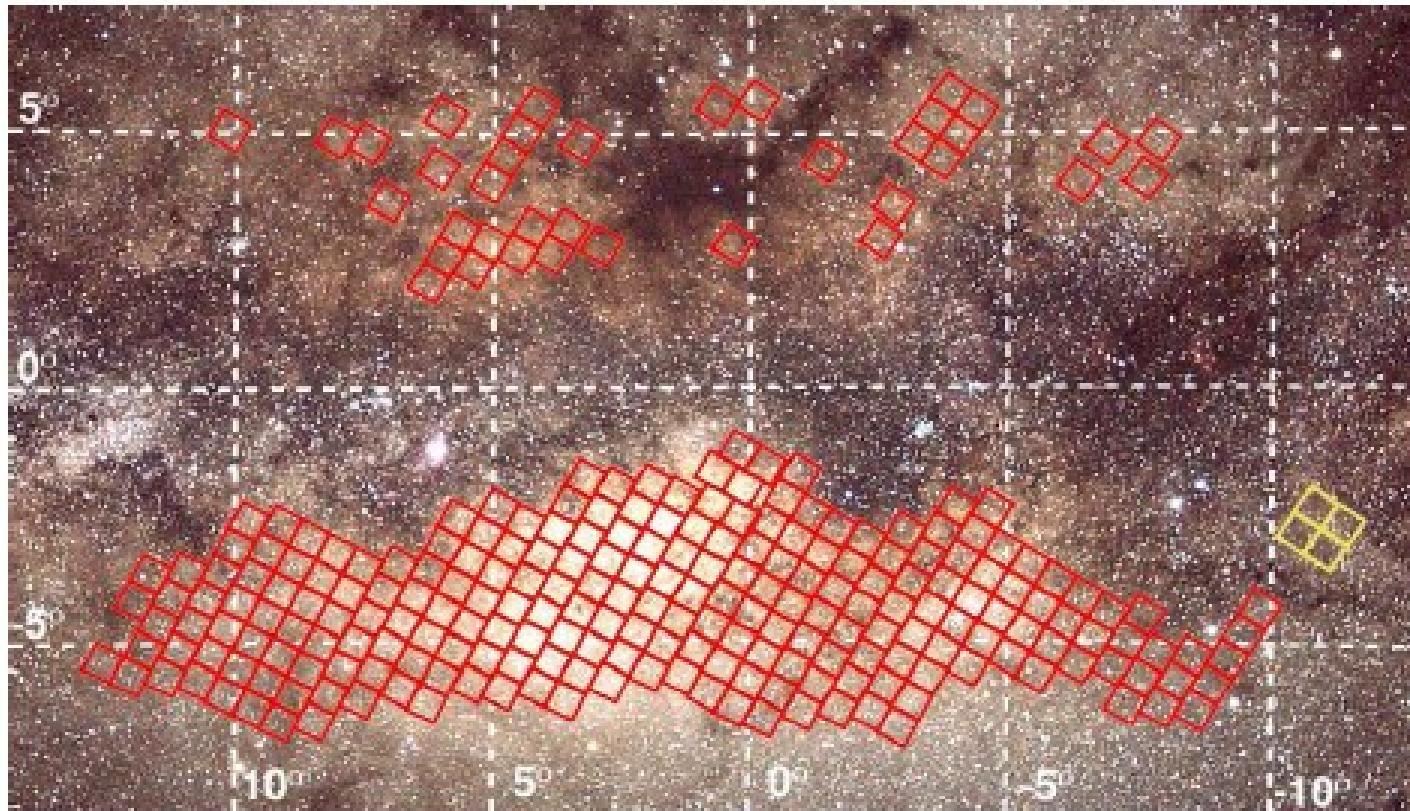


# Needed to measure $\theta_E$ :

## Standard Sky-Plane Rulers

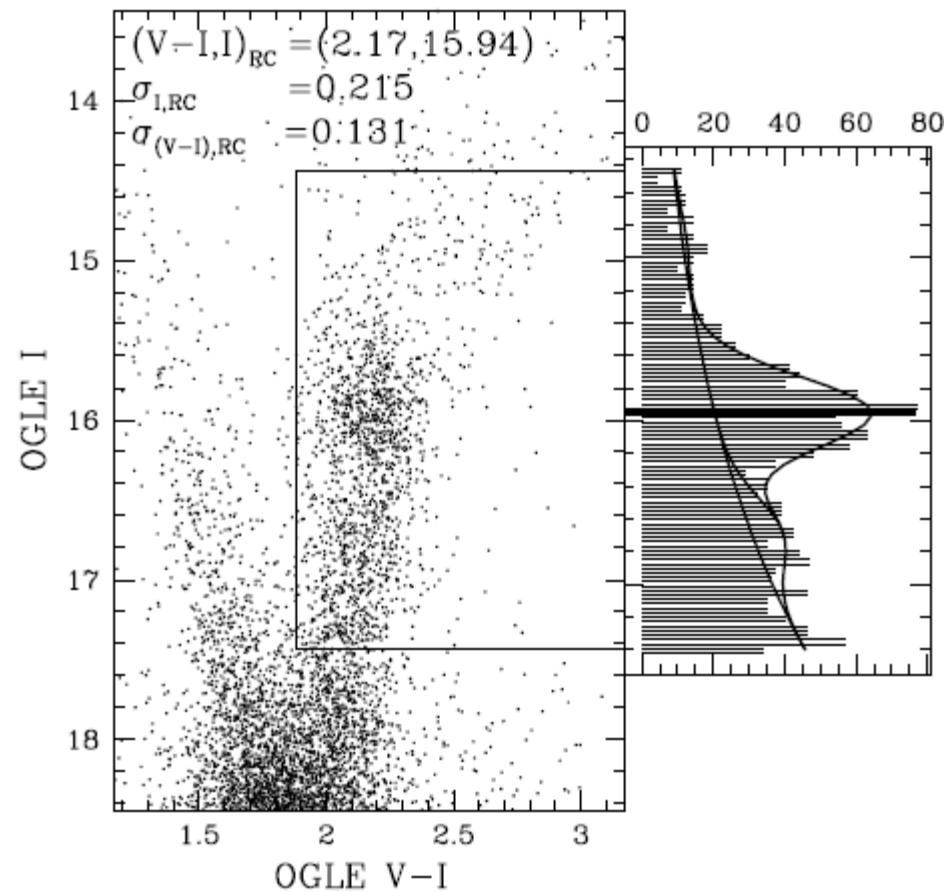


# Clump: Standard Candle Probe of Bulge



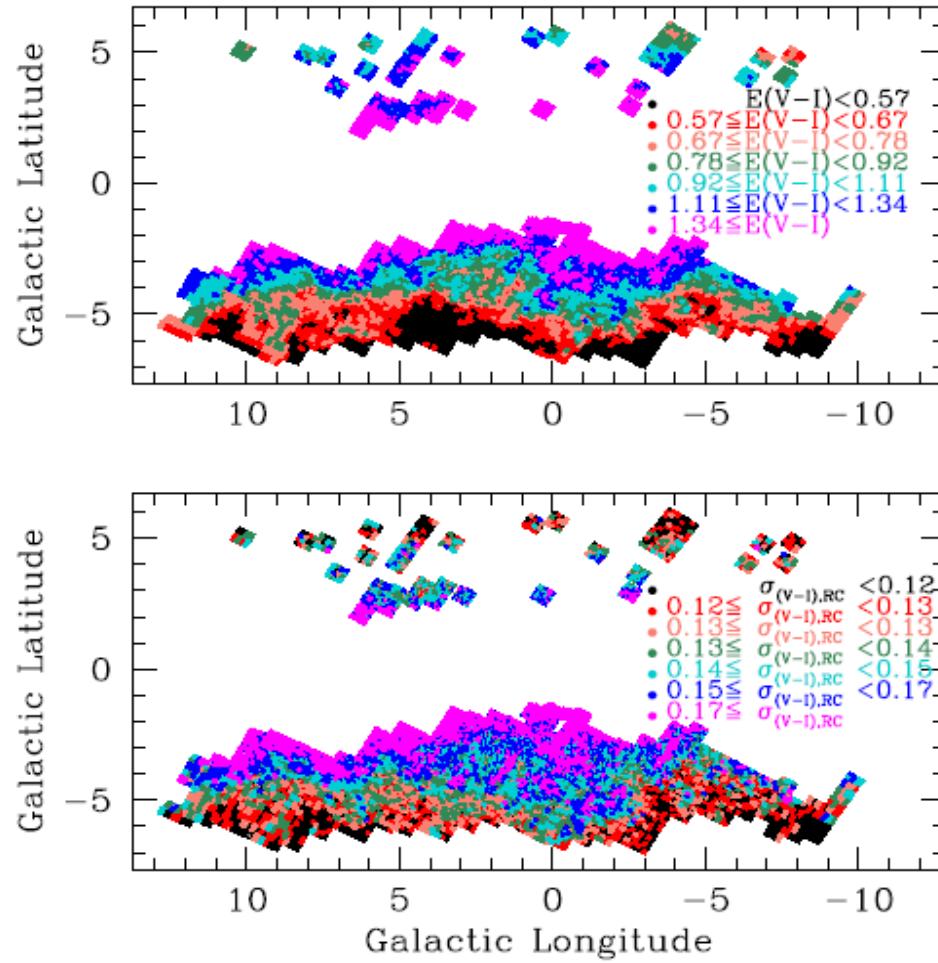
Nataf et al. 2013, ApJ, 769, 88

# Clump: Standard Candle Probe of Bulge



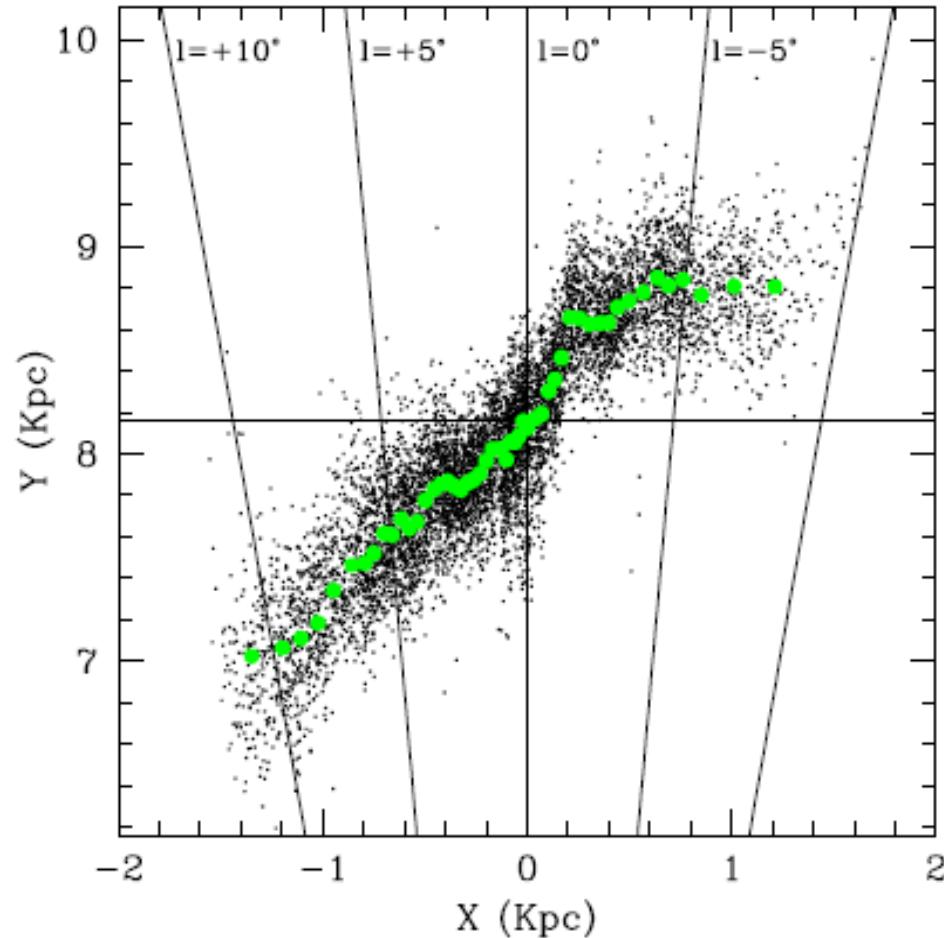
Nataf et al. 2013, ApJ, 769, 88

# Clump: Extinction Probe



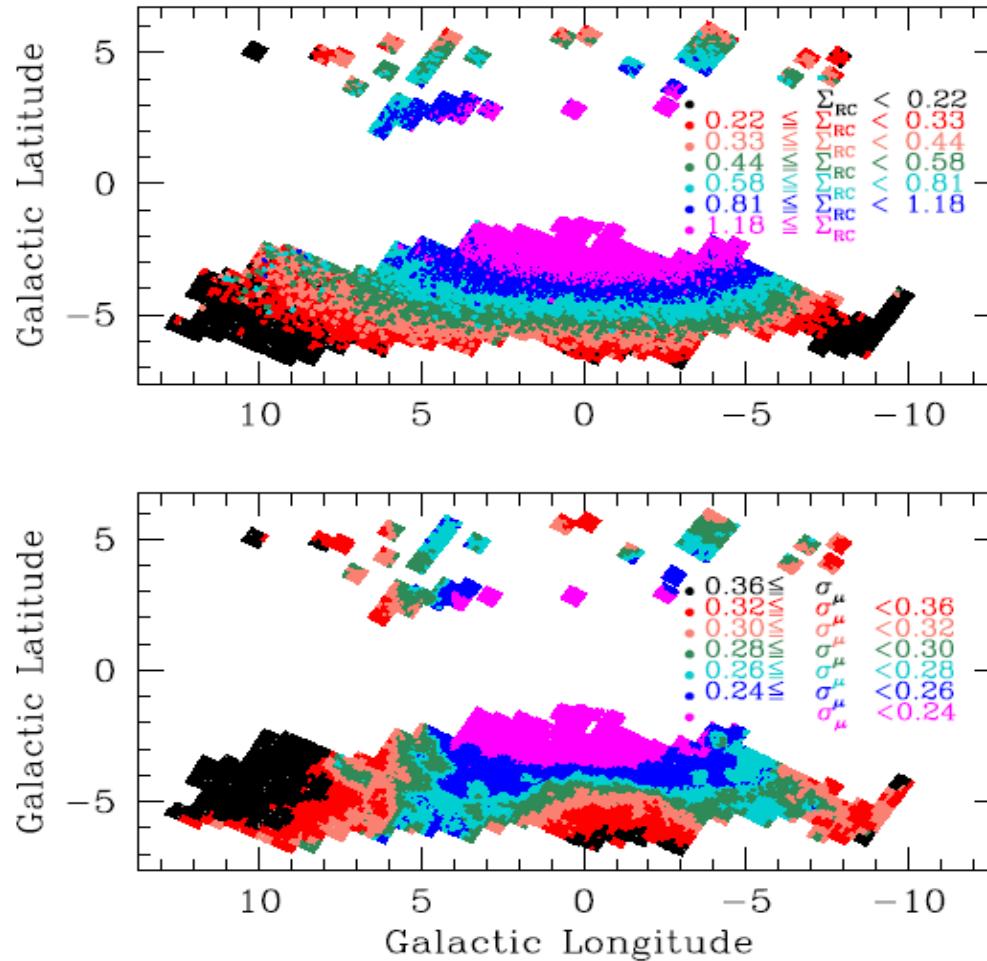
Nataf et al. 2013, ApJ, 769, 88

# Clump: Distance Probe



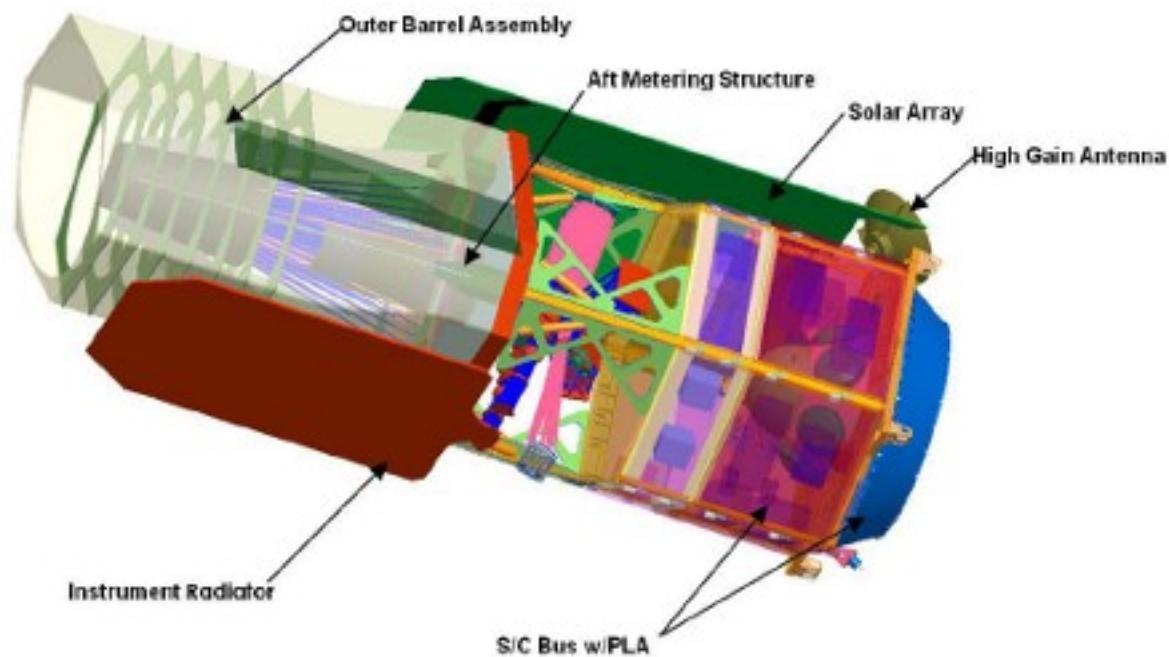
Nataf et al. 2013, ApJ, 769, 88

# Clump: Density and Depth Probes

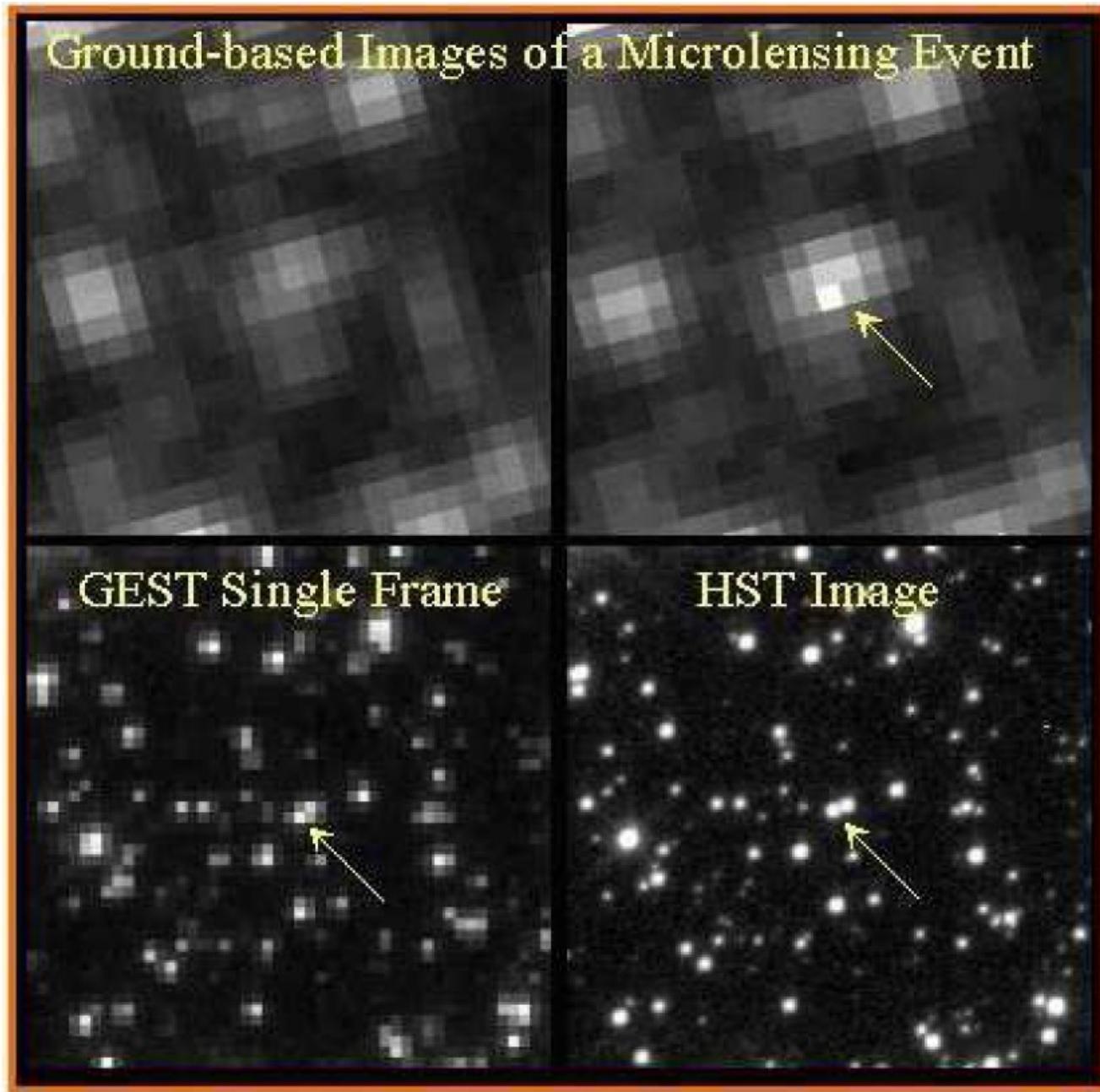


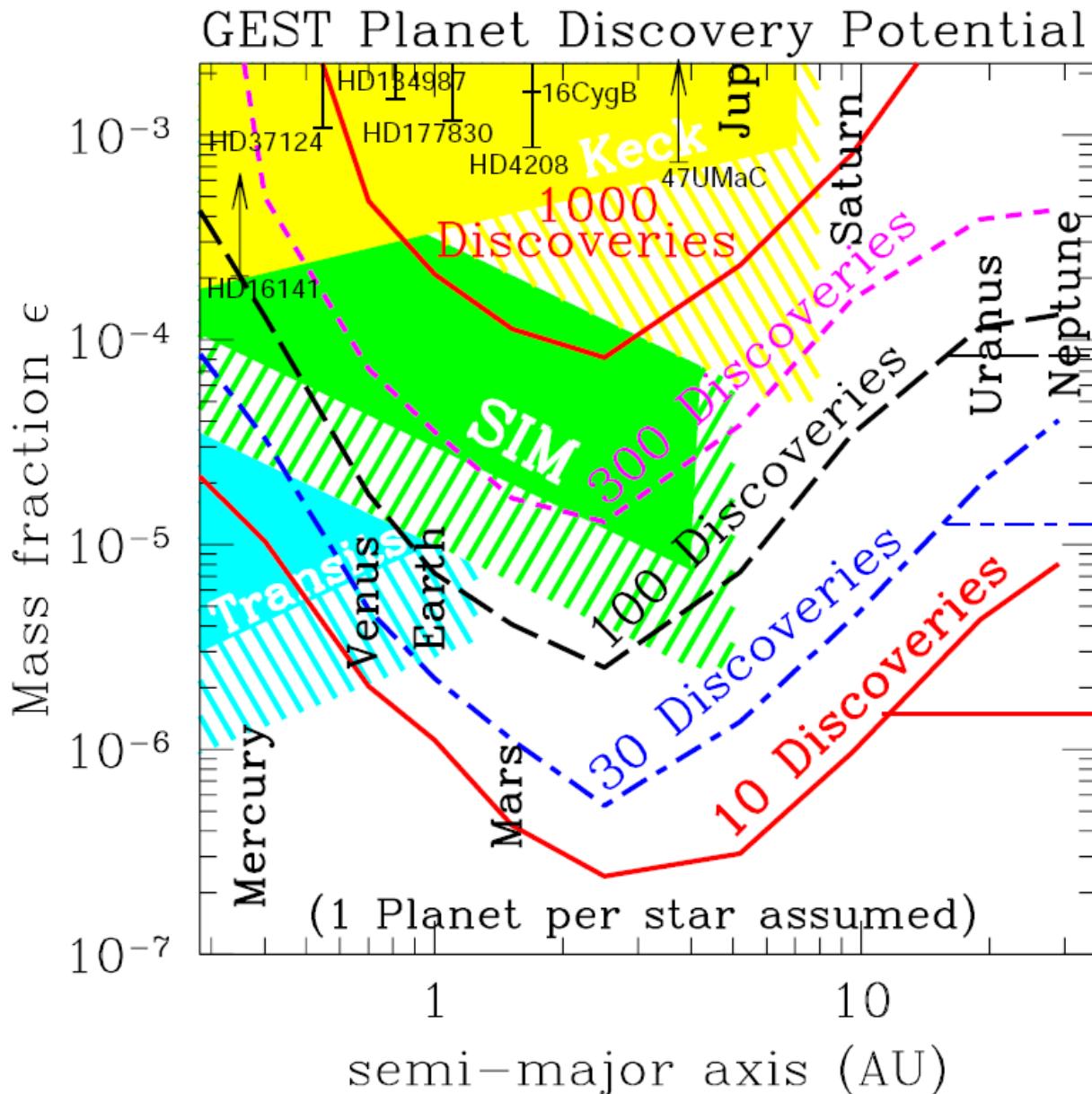
Nataf et al. 2013, ApJ, 769, 88

# WFIRST



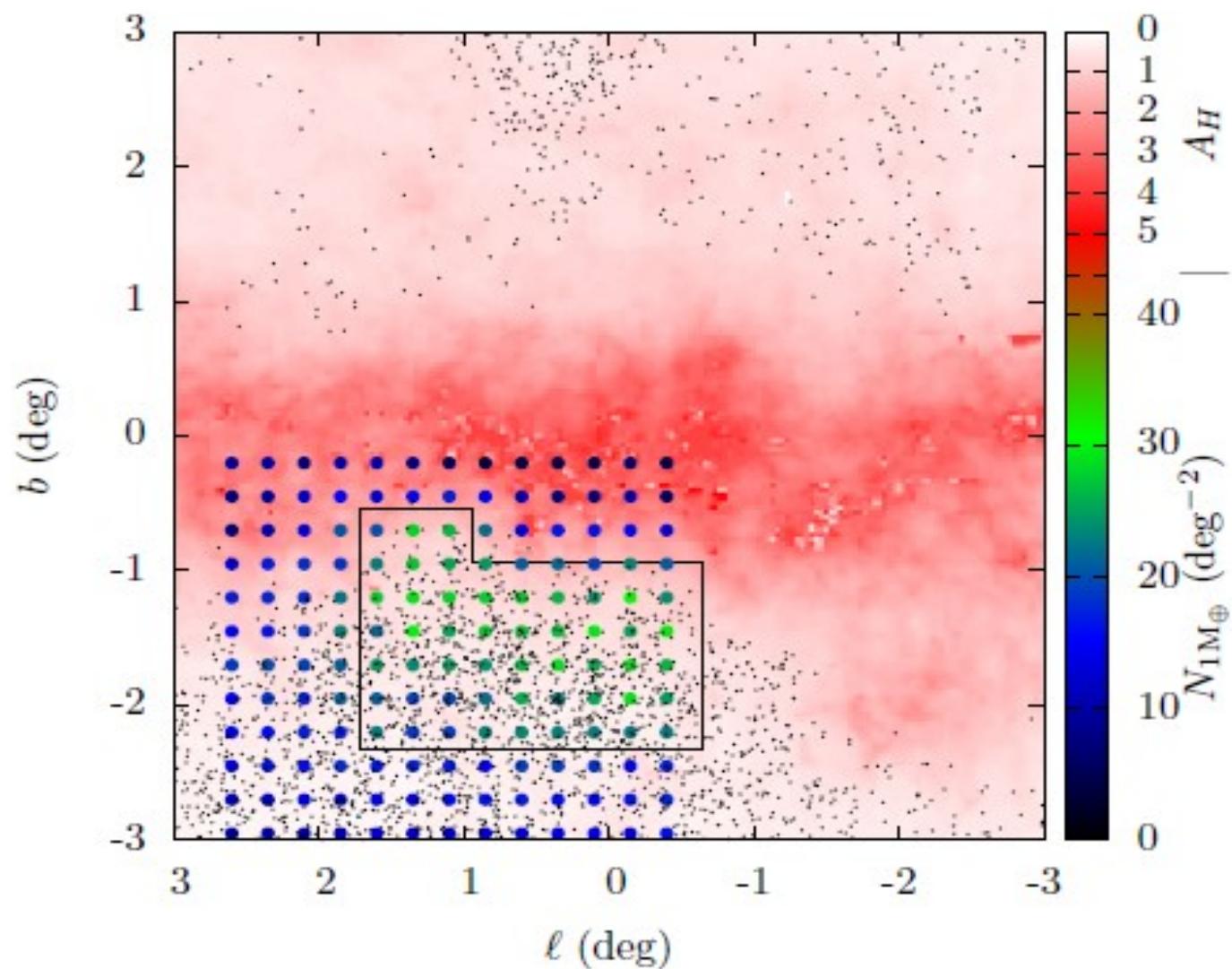
# Seeing Better In Space (also weather)





Bennett & Rhei 2002, ApJ, 574, 985

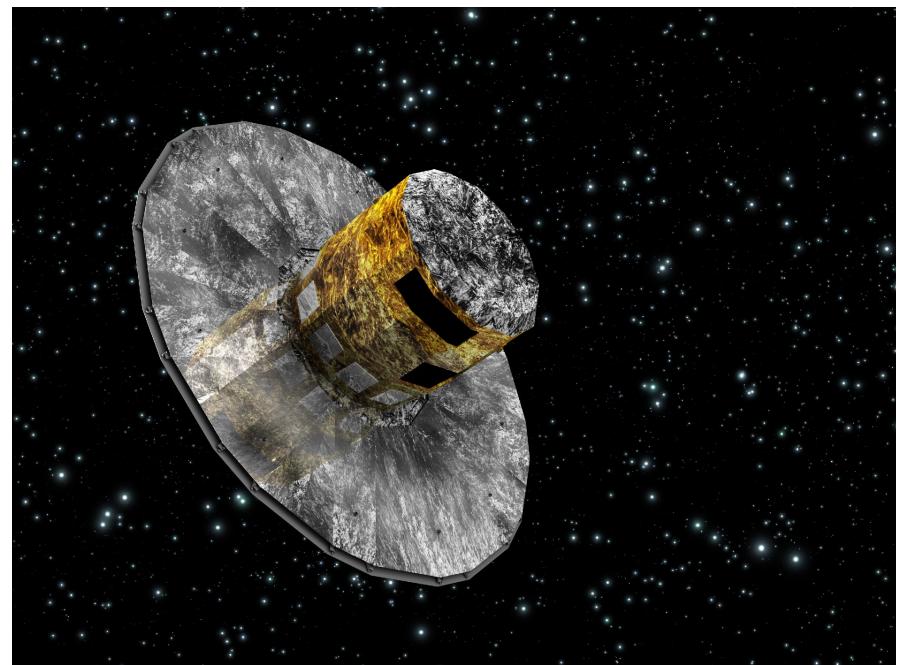
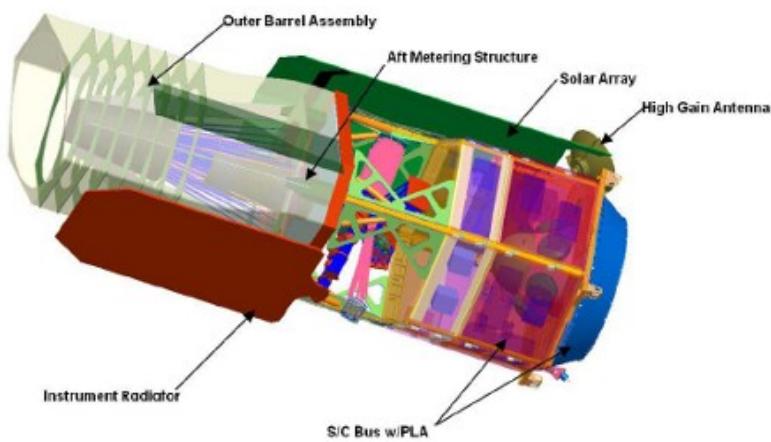
# WFIRST Microlensing Field



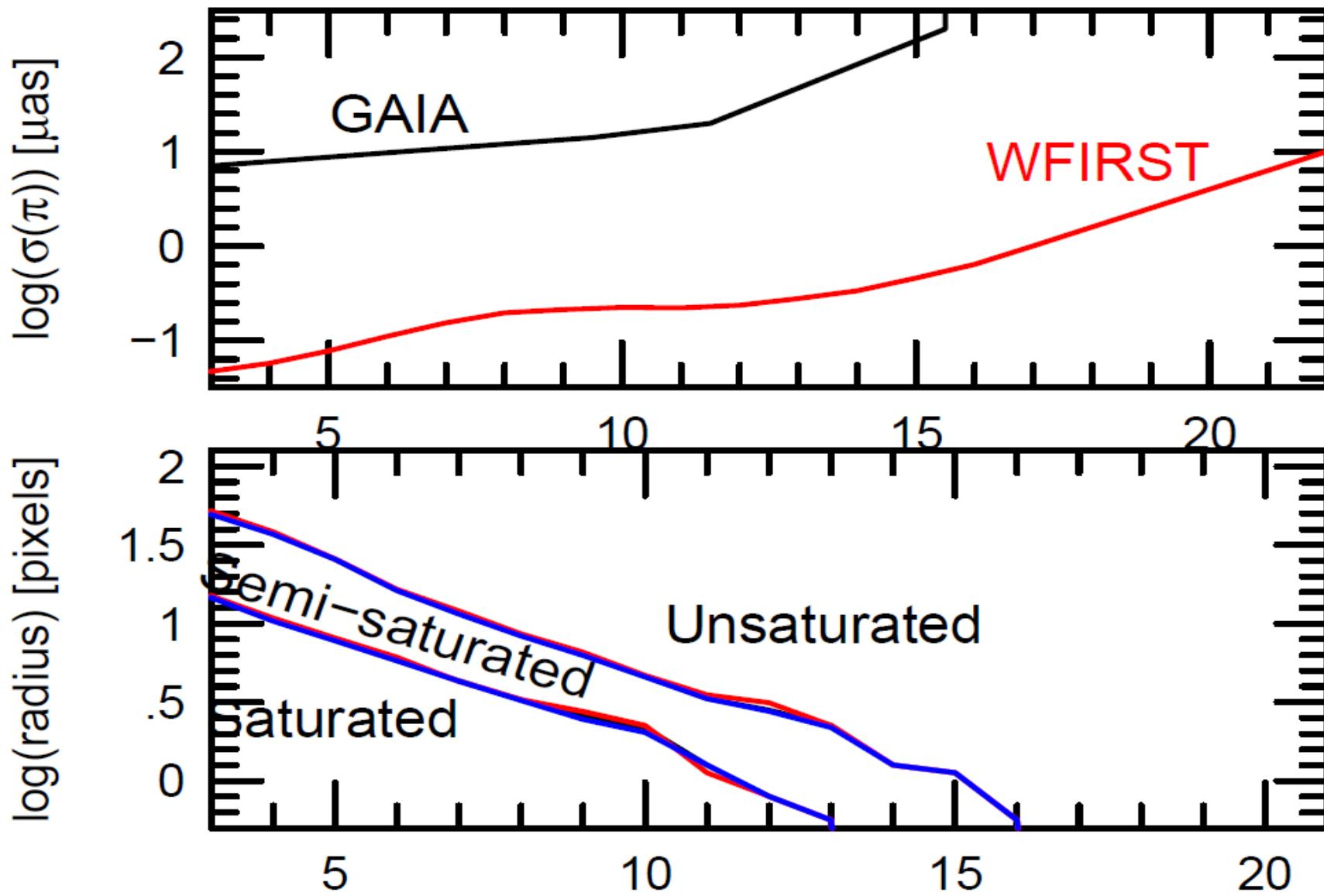
# WFIRST “Microlensing” Survey Characteristics

- 40,000 images (52 sec)
- 2.8 sq.deg.
- 6 continuous 72-day campaigns (at quadrature)
- 100 images per day
- $\text{SNR} = 10^{\{0.4(\text{Hzero}-\text{H})\}}$  Hzero = 26.1

# WFIRST vs. GAIA



# WFIRST vs GAIA Parallax Precision



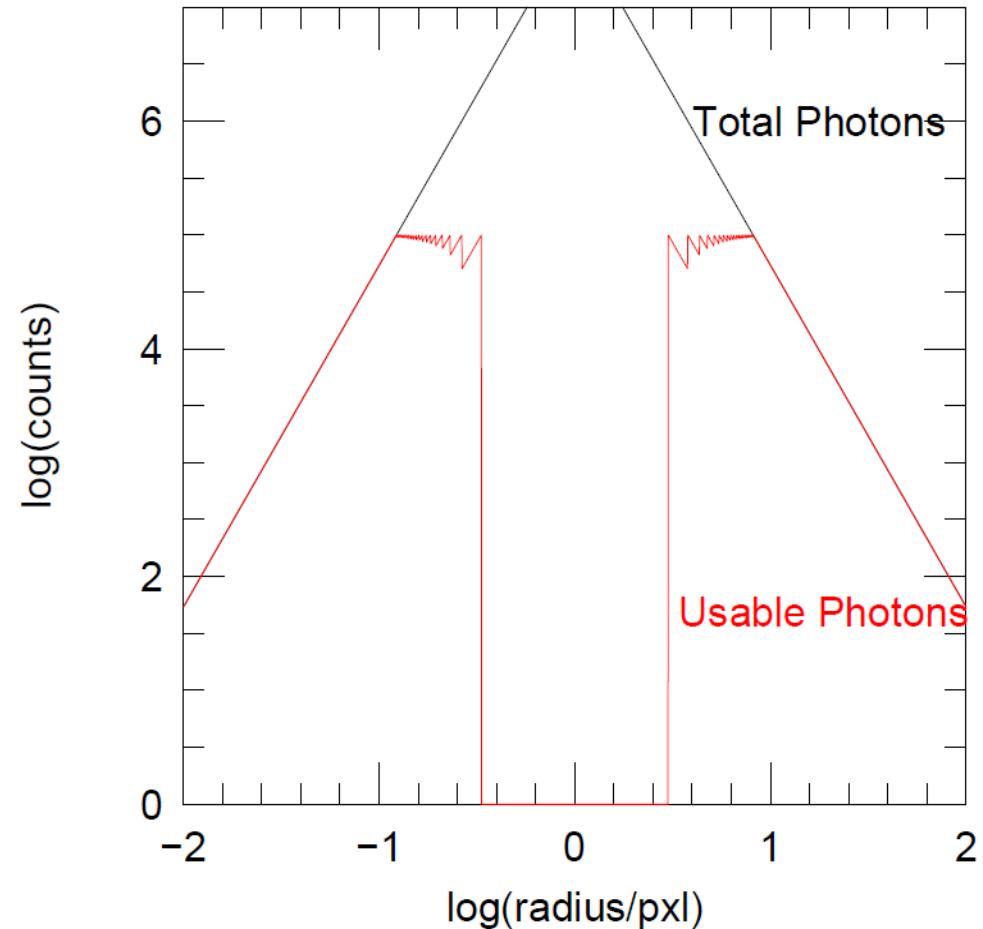
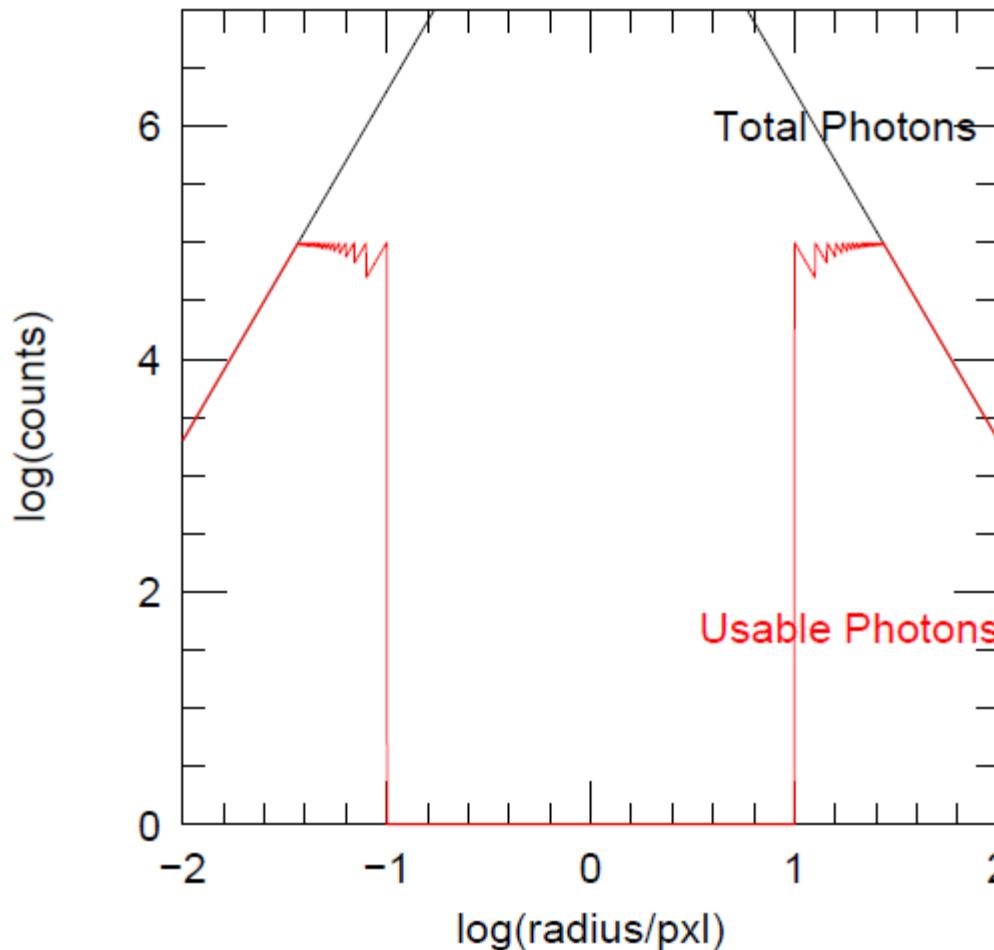
# Non-Microlensing WFIRST Science: Ultra-precise Parallaxes

- $H < 14.0$ ;  $\sigma(\pi) < 0.3 \mu\text{as}$ ; 1,000,000 stars
- $H < 19.6$ ;  $\sigma(\pi) < 3.7 \mu\text{as}$ ; 40,000,000 stars
- $H < 21.6$ ;  $\sigma(\pi) < 10 \mu\text{as}$ ; 120,000,000 stars

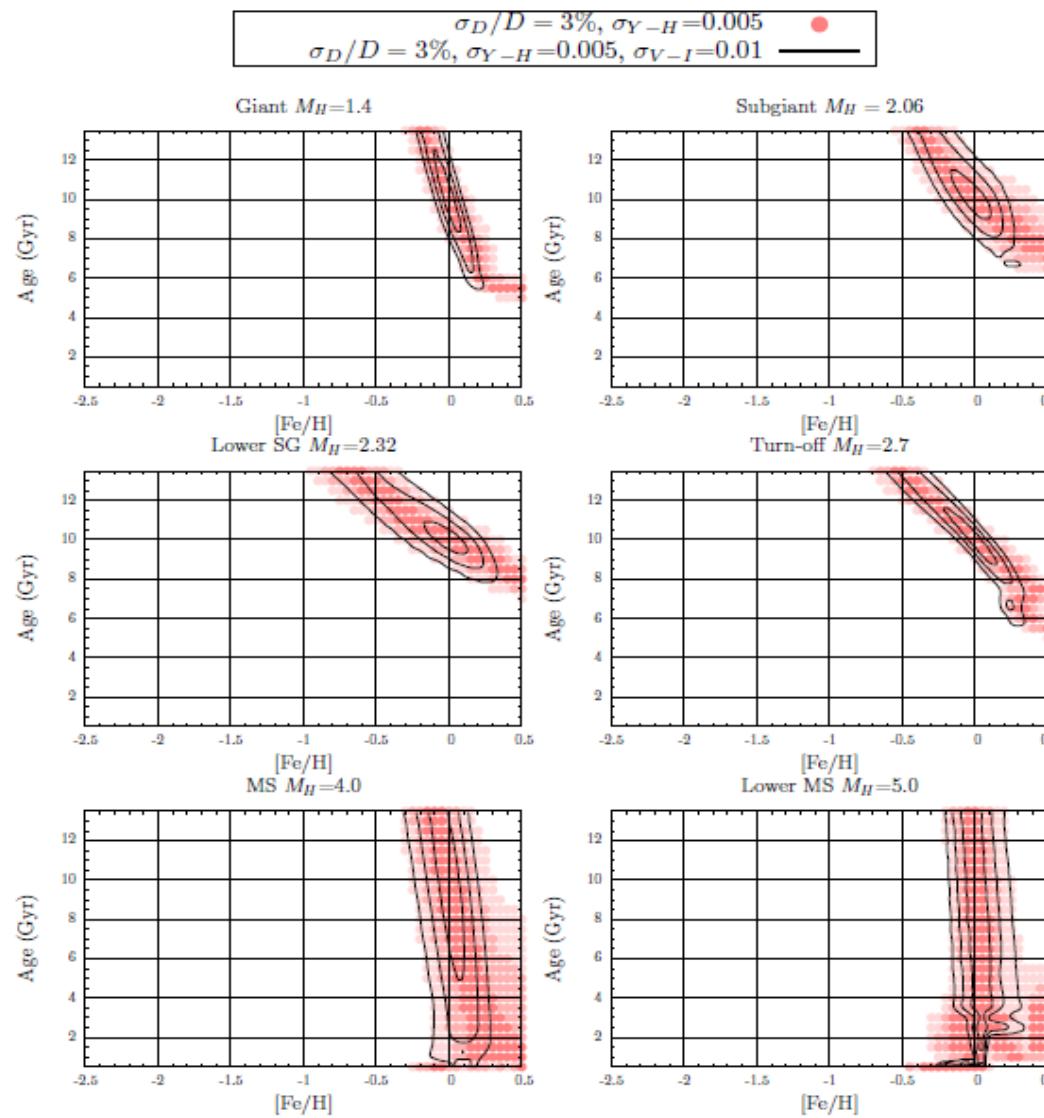
Gould, Huber, Penny, Stello, 2015 JKAS, in press

# WFIRST

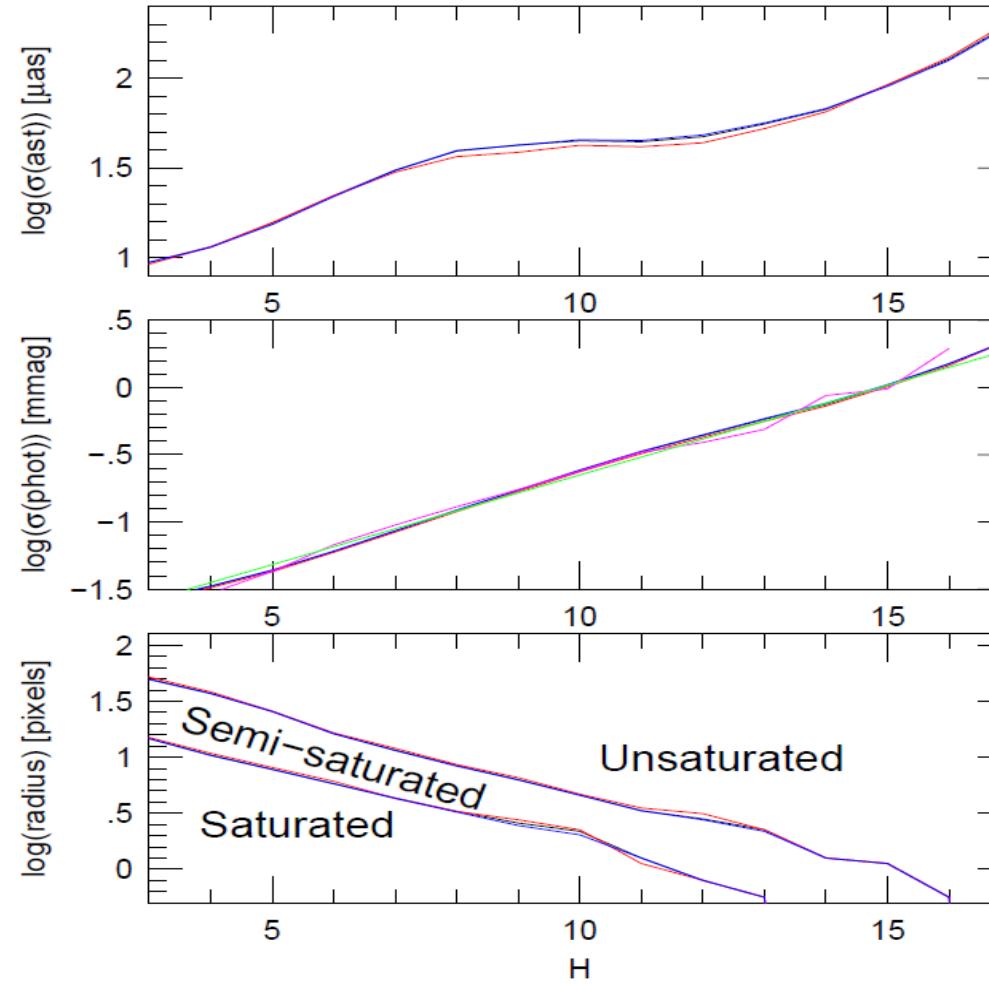
## Astrometric Information Flow



# Age & [Fe/H] for 7,000,000 stars (first four panels) [needs V/I-band]

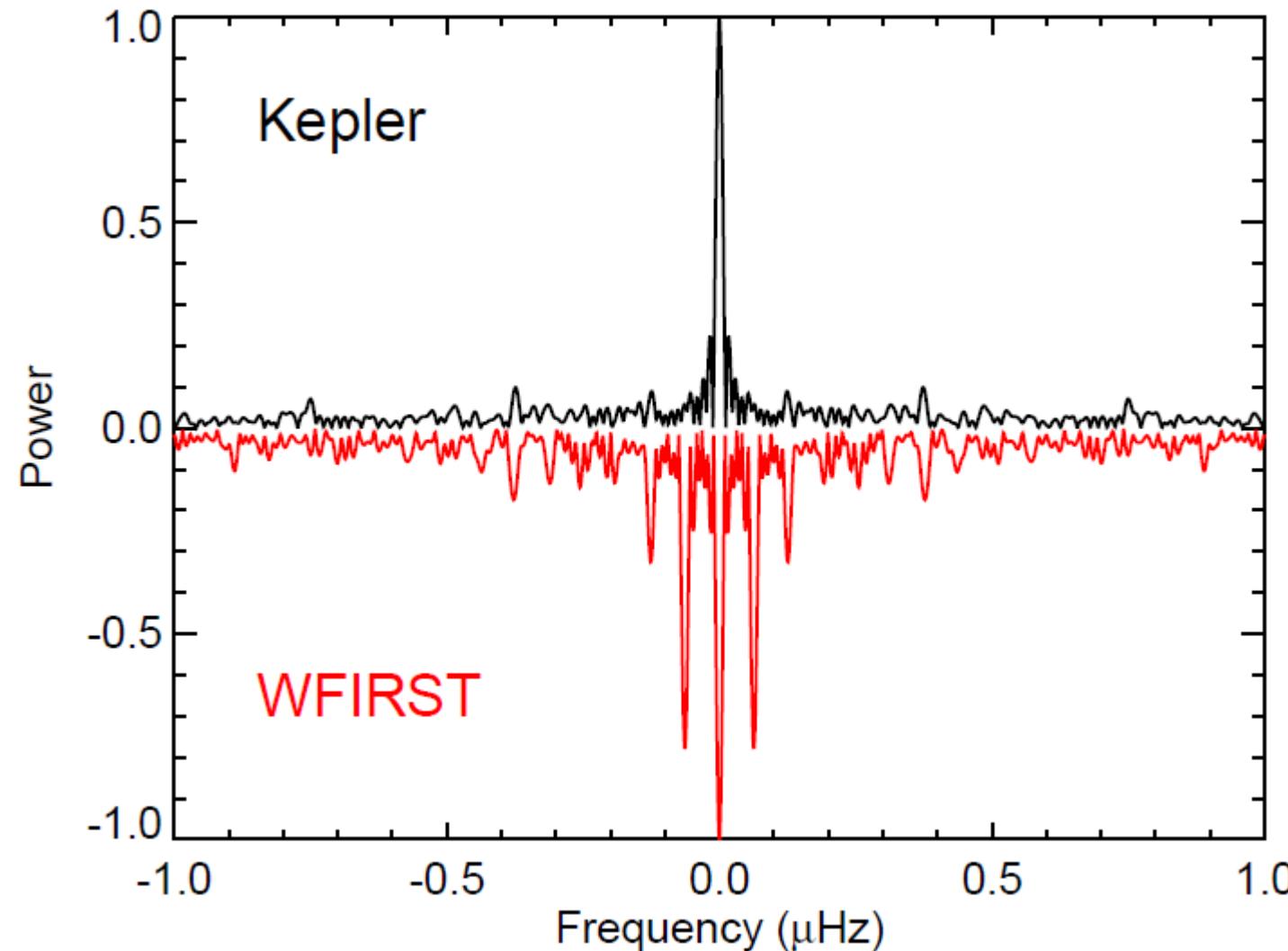


# Non-Microlensing WFIRST Science: Ultra-precise Parallaxes and Photometry



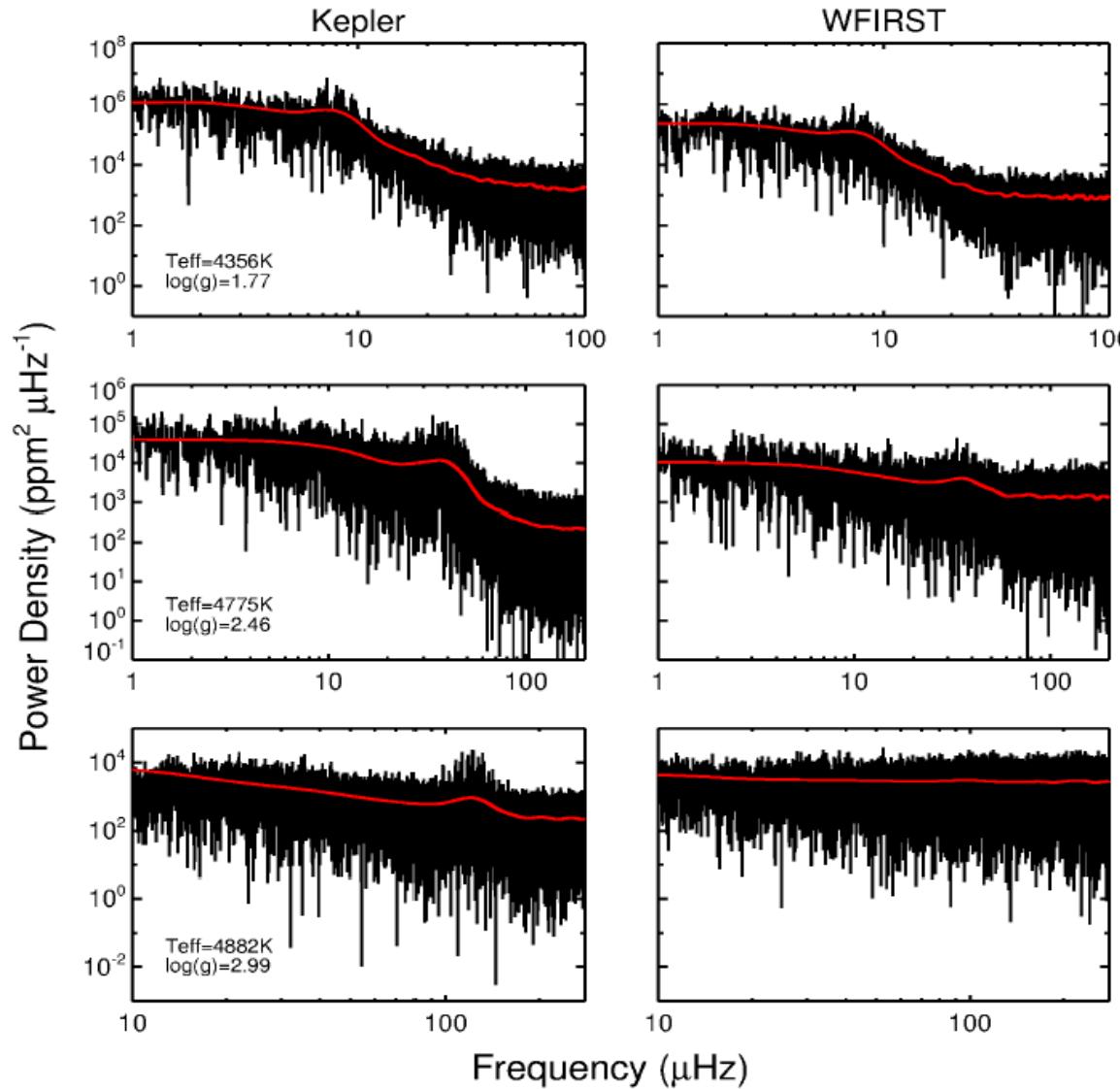
Gould, Huber, Penny, Stello, 2015 JKAS, 48, 93

# Non-Microlensing WFIRST Science: Asteroseismic Window Function

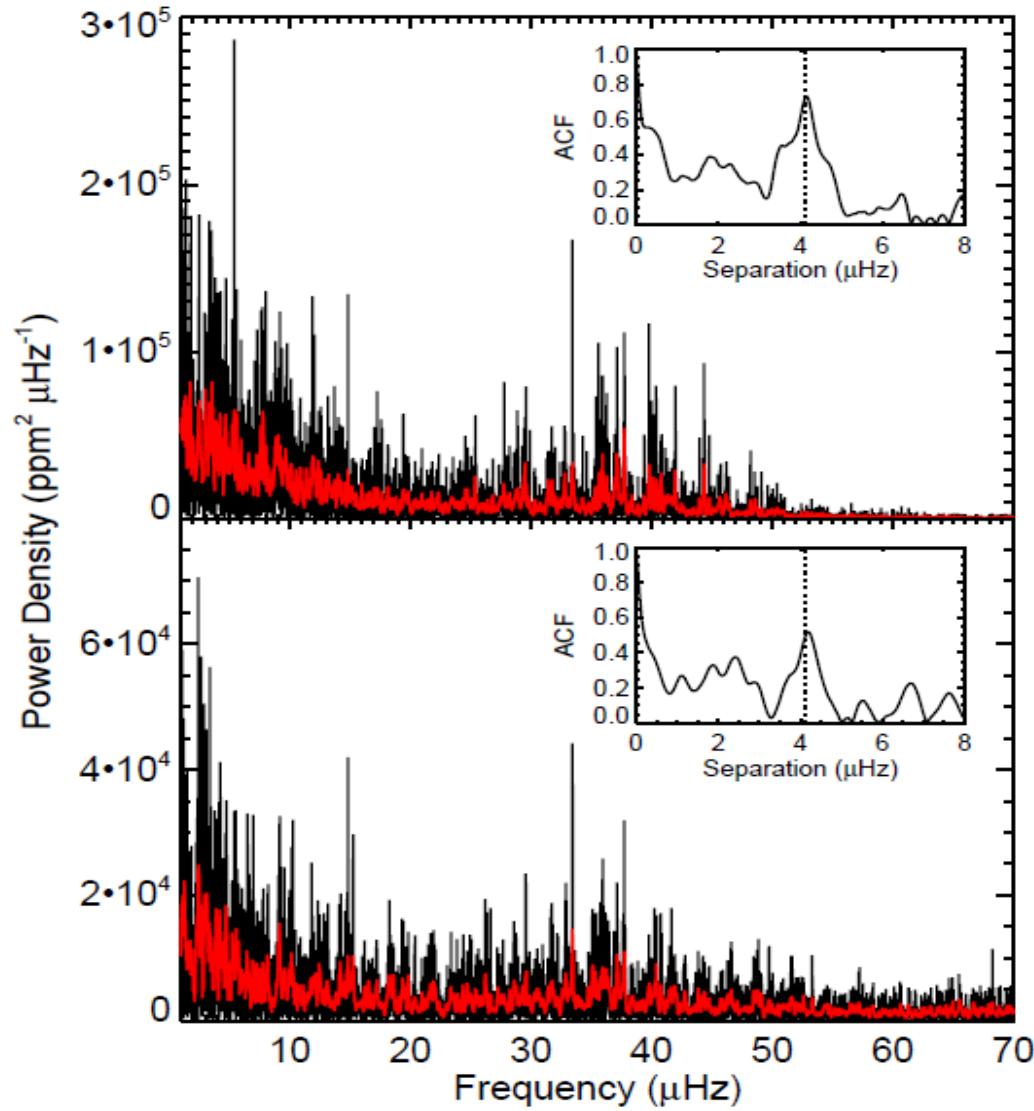


Gould, Huber, Penny, Stello, 2015, JKAS, 48, 93

# Non- $\mu$ lens WFIRST Science: $v_{\max}$



# Non- $\mu$ lens WFIRST Science: $\Delta v$



Gould, Huber, Penny, Stello, 2015, JKAS, 48, 93

$$\Delta\nu \,\&\, \nu_{\mathrm{max}}$$

$$\frac{\rho}{\rho_\odot} \simeq \left(\frac{\langle \Delta\nu_{nl}\rangle}{\langle \Delta\nu_{nl}\rangle_\odot}\right)^2, \qquad \frac{g}{g_\odot} \simeq \frac{\nu_{\mathrm{max}}}{\nu_{\mathrm{max},\odot}} \left(\frac{T_{\mathrm{eff}}}{T_{\mathrm{eff},\odot}}\right)^{1/2}$$

# $\Delta\nu$ & $\nu_{\text{max}}$

$$\frac{\rho}{\rho_{\odot}} \simeq \left( \frac{\langle \Delta\nu_{nl} \rangle}{\langle \Delta\nu_{nl} \rangle_{\odot}} \right)^2, \quad \frac{g}{g_{\odot}} \simeq \frac{\nu_{\text{max}}}{\nu_{\text{max},\odot}} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{1/2}$$

$$\frac{R}{R_{\odot}} \simeq \frac{\nu_{\text{max}}}{\nu_{\text{max},\odot}} \left( \frac{\langle \Delta\nu_{nl} \rangle}{\langle \Delta\nu_{nl} \rangle_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{1/2}$$

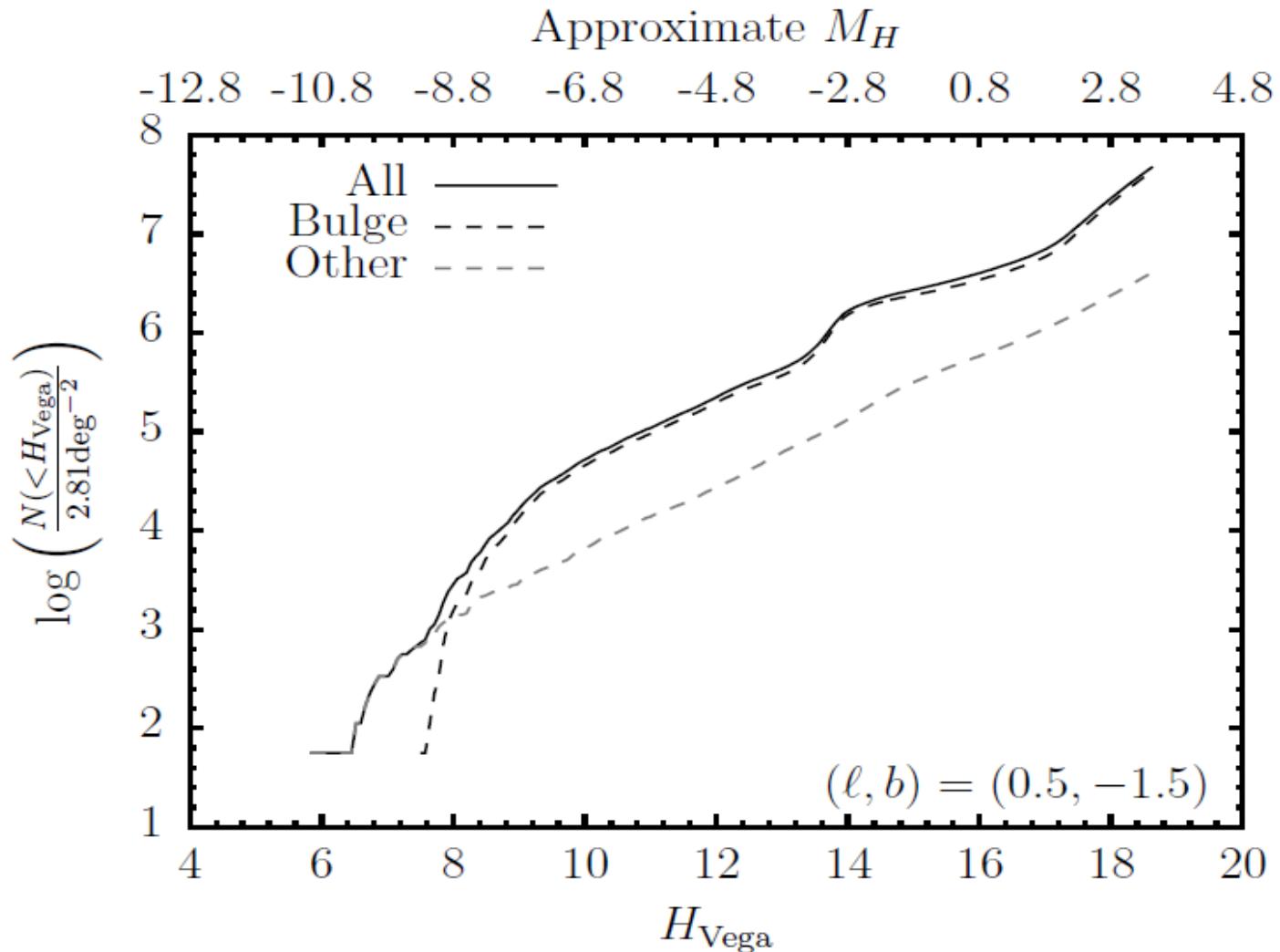
# $\Delta\nu$ & $\nu_{\text{max}}$

$$\frac{\rho}{\rho_{\odot}} \simeq \left( \frac{\langle \Delta\nu_{nl} \rangle}{\langle \Delta\nu_{nl} \rangle_{\odot}} \right)^2, \quad \frac{g}{g_{\odot}} \simeq \frac{\nu_{\text{max}}}{\nu_{\text{max},\odot}} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{1/2}$$

$$\frac{R}{R_{\odot}} \simeq \frac{\nu_{\text{max}}}{\nu_{\text{max},\odot}} \left( \frac{\langle \Delta\nu_{nl} \rangle}{\langle \Delta\nu_{nl} \rangle_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{1/2}$$

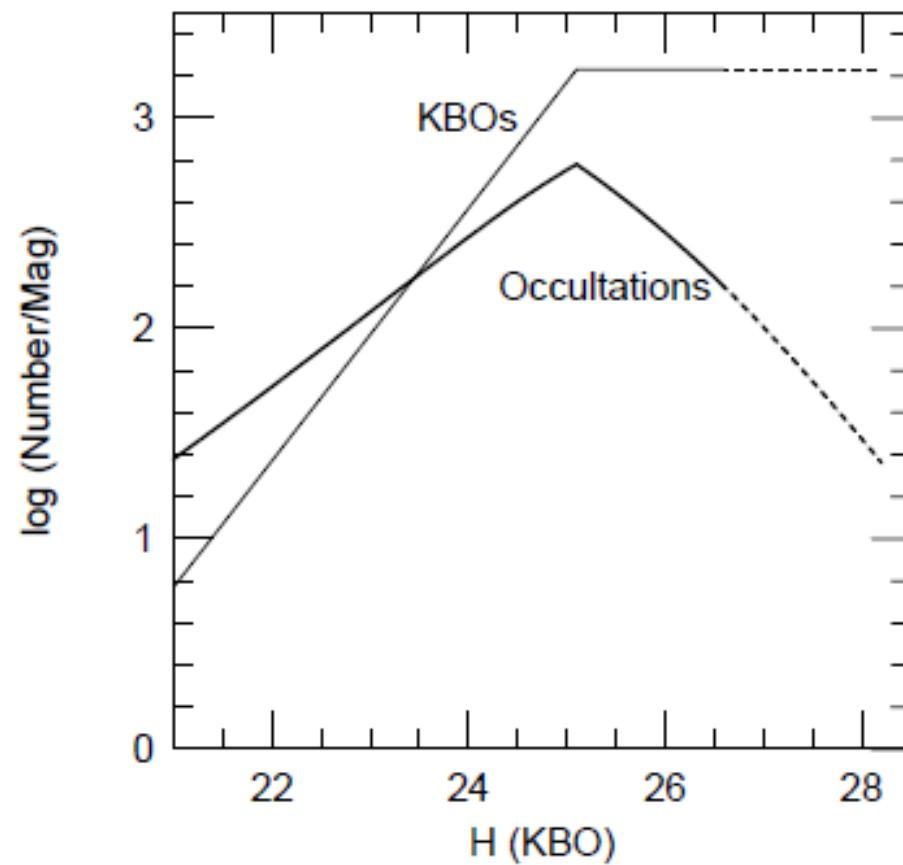
$$\frac{M}{M_{\odot}} \simeq \left( \frac{\nu_{\text{max}}}{\nu_{\text{max},\odot}} \right)^3 \left( \frac{\langle \Delta\nu_{nl} \rangle}{\langle \Delta\nu_{nl} \rangle_{\odot}} \right)^{-4} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{3/2}$$

# Non- $\mu$ lens WFIRST Science: 10% Disk Stars



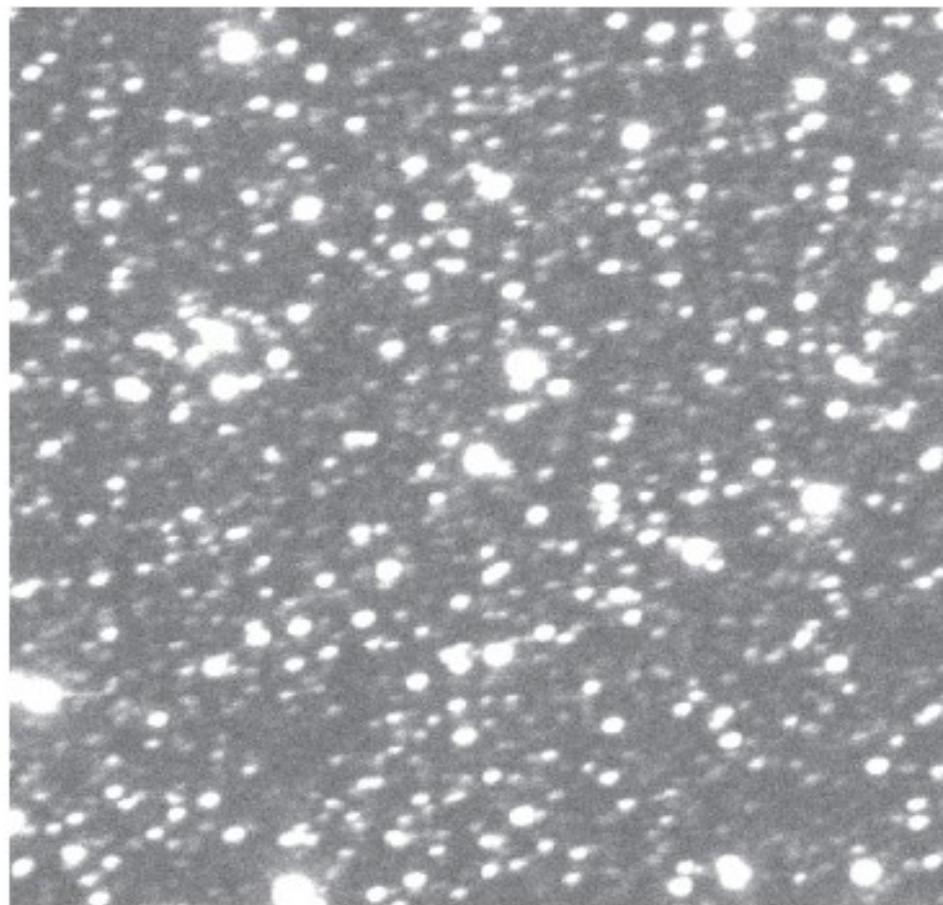
Gould, Huber, Penny, Stello, 2015, JKAS, 48, 93

# Non- $\mu$ lens WFIRST Science: KBOs



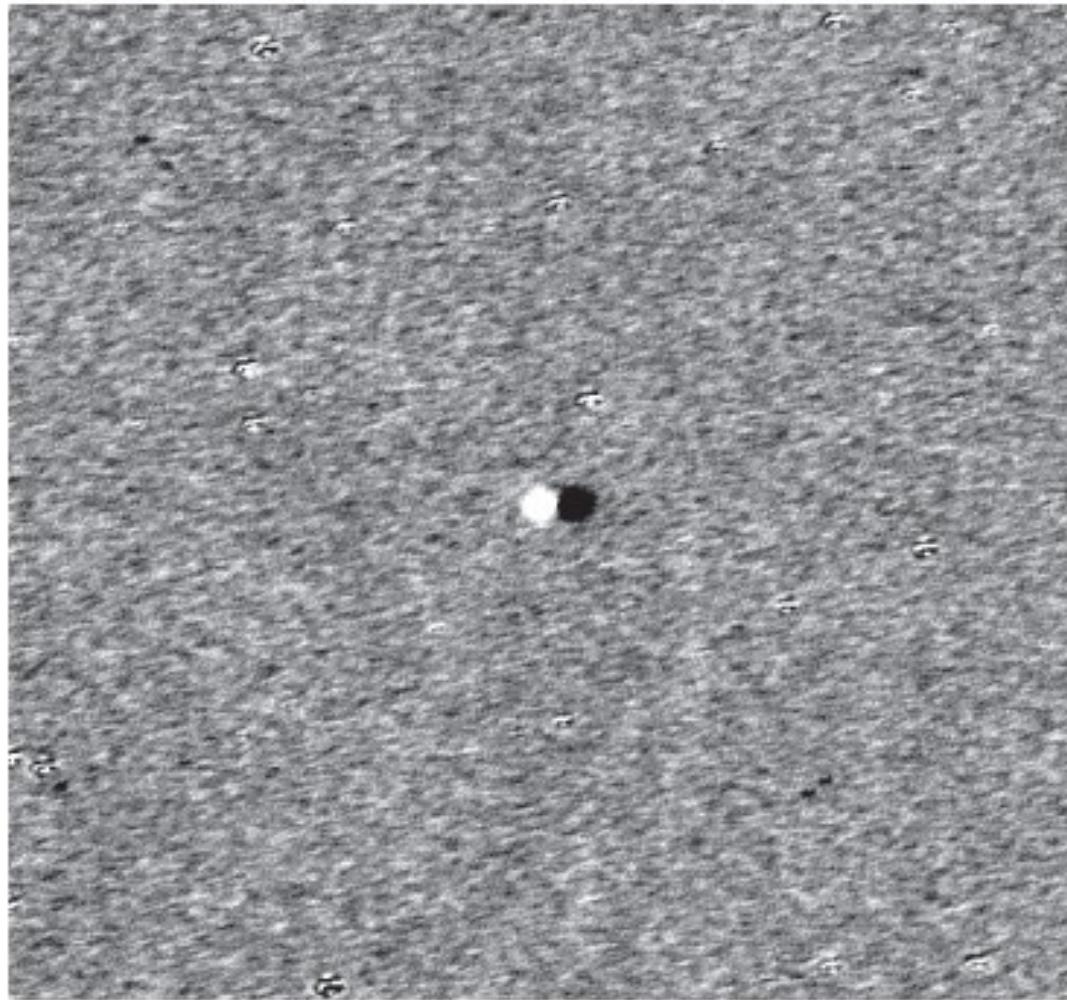
Gould 2014 JKAS, 47, 279

# KBOs possible in microlensing fields?



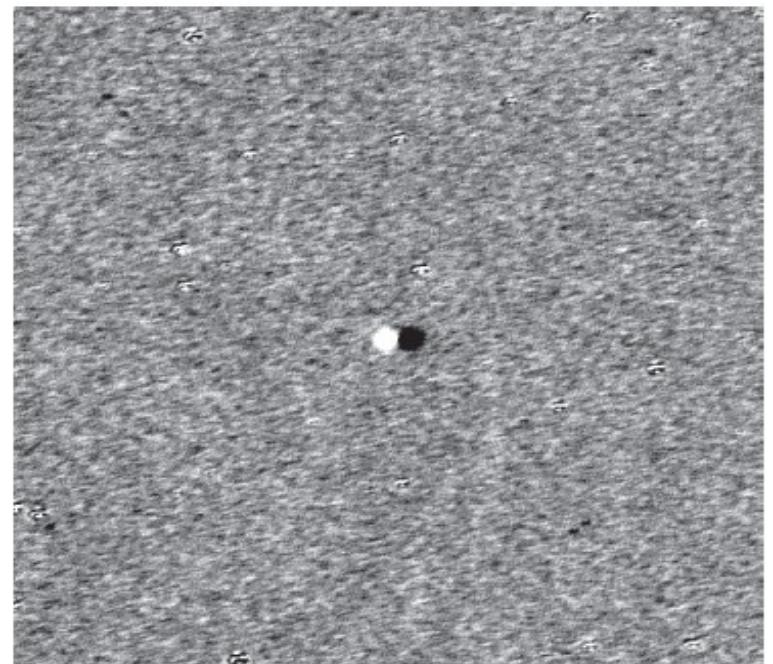
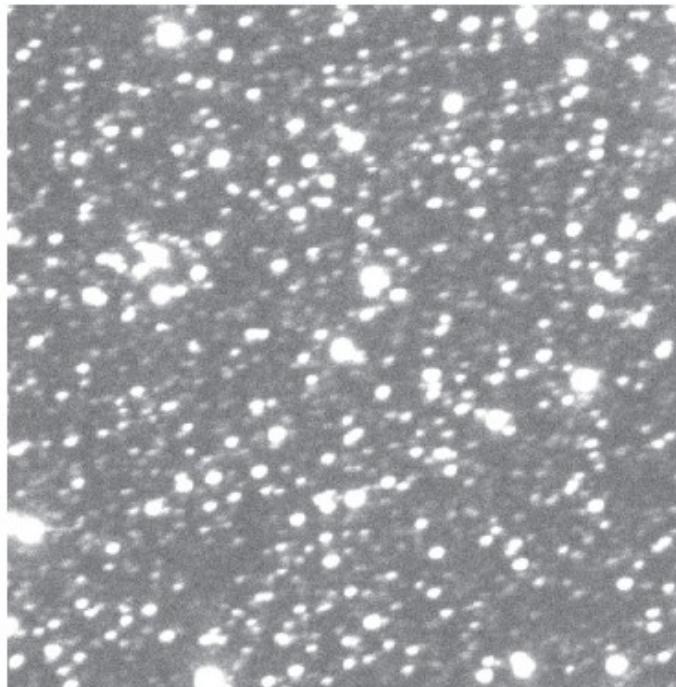
Shepard et al. 2011, AJ, 142, 98

Yes! Microlensing fields  
are not crowded ...



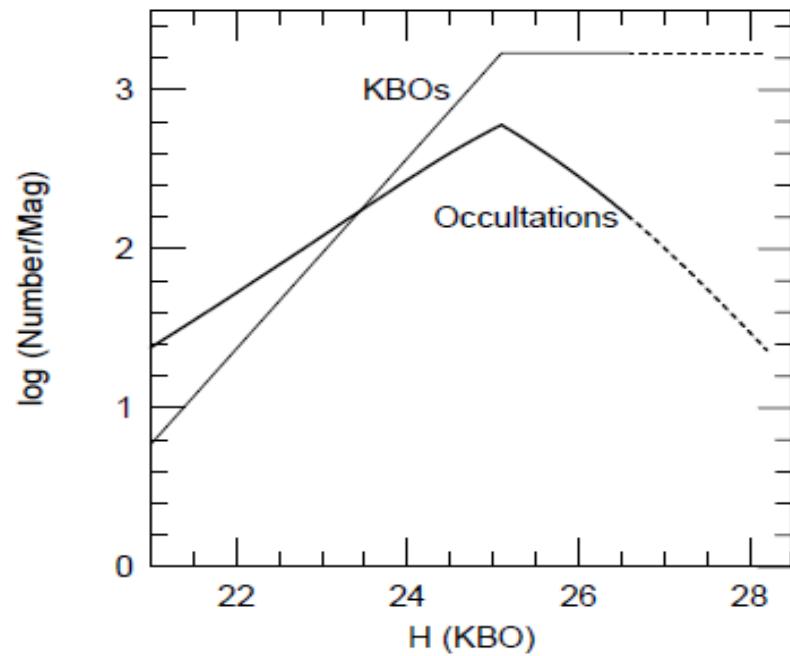
Sheppard et al. 2011, AJ, 142, 98

Yes! Microlensing fields are not crowded  
after image subtraction!



Sheppard et al. 2011, AJ, 142, 98

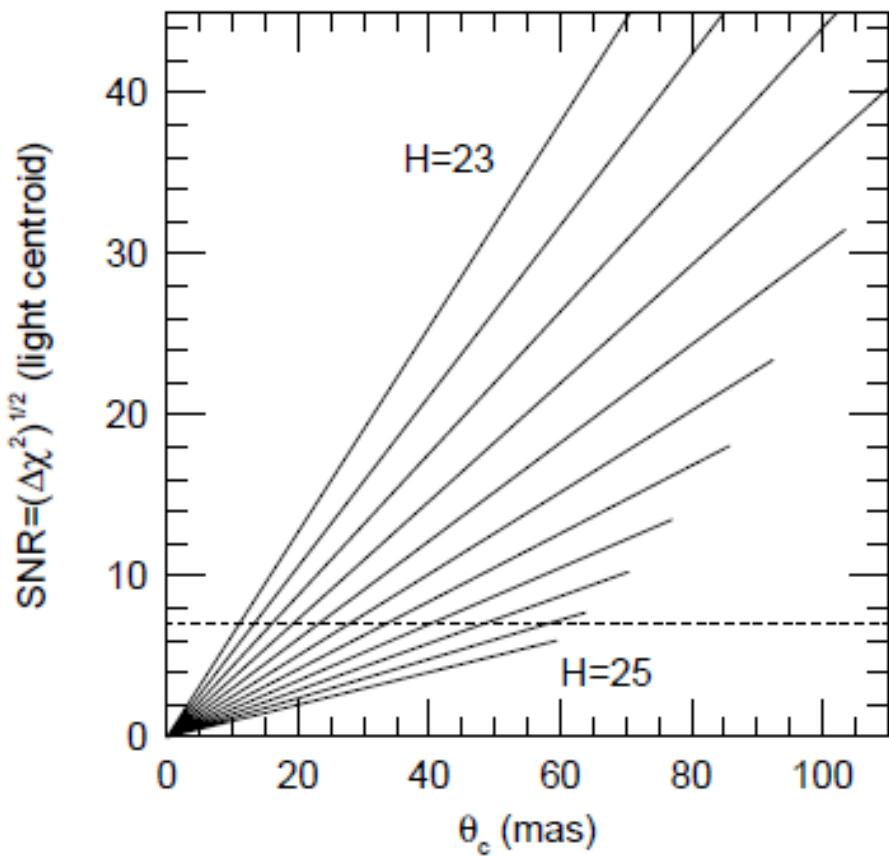
# Non- $\mu$ lens WFIRST Science: KBO Precision orbits



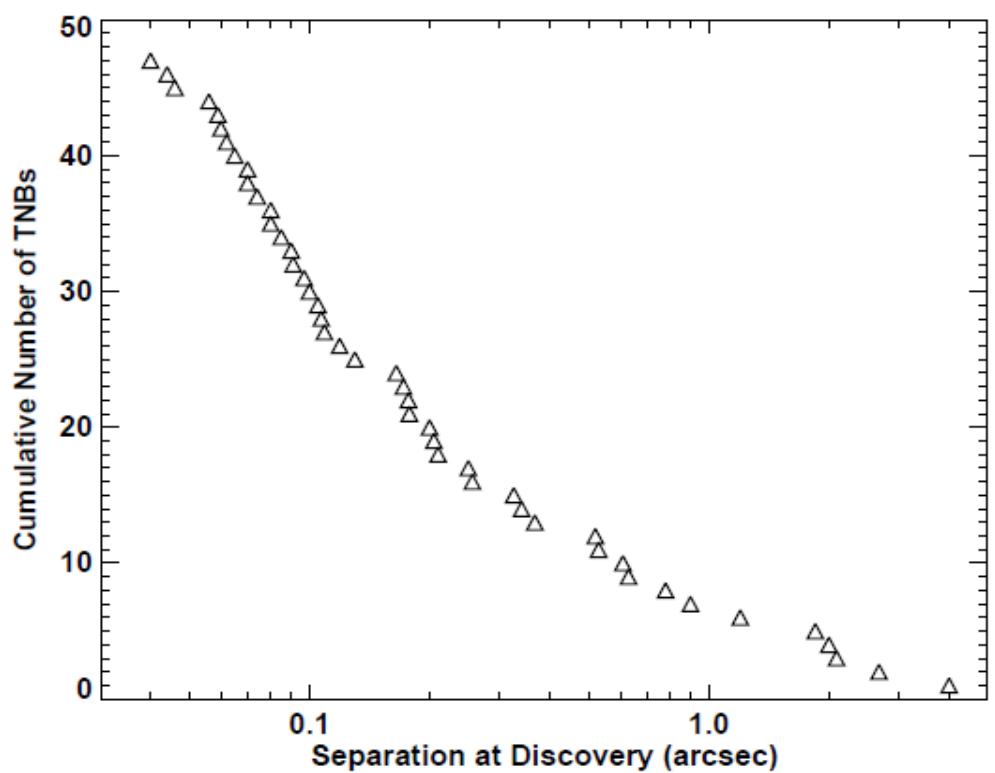
$$\sigma(P)/P \sim 0.09\%$$

H ~ 25.1

# Non- $\mu$ lens WFIRST Science: KBO Binaries



Gould 2014 JKAS, 47, 279



Noll et al. 2008

# Non- $\mu$ lens WFIRST Science: Transits: -> Galactic Distribution of Hot Planets

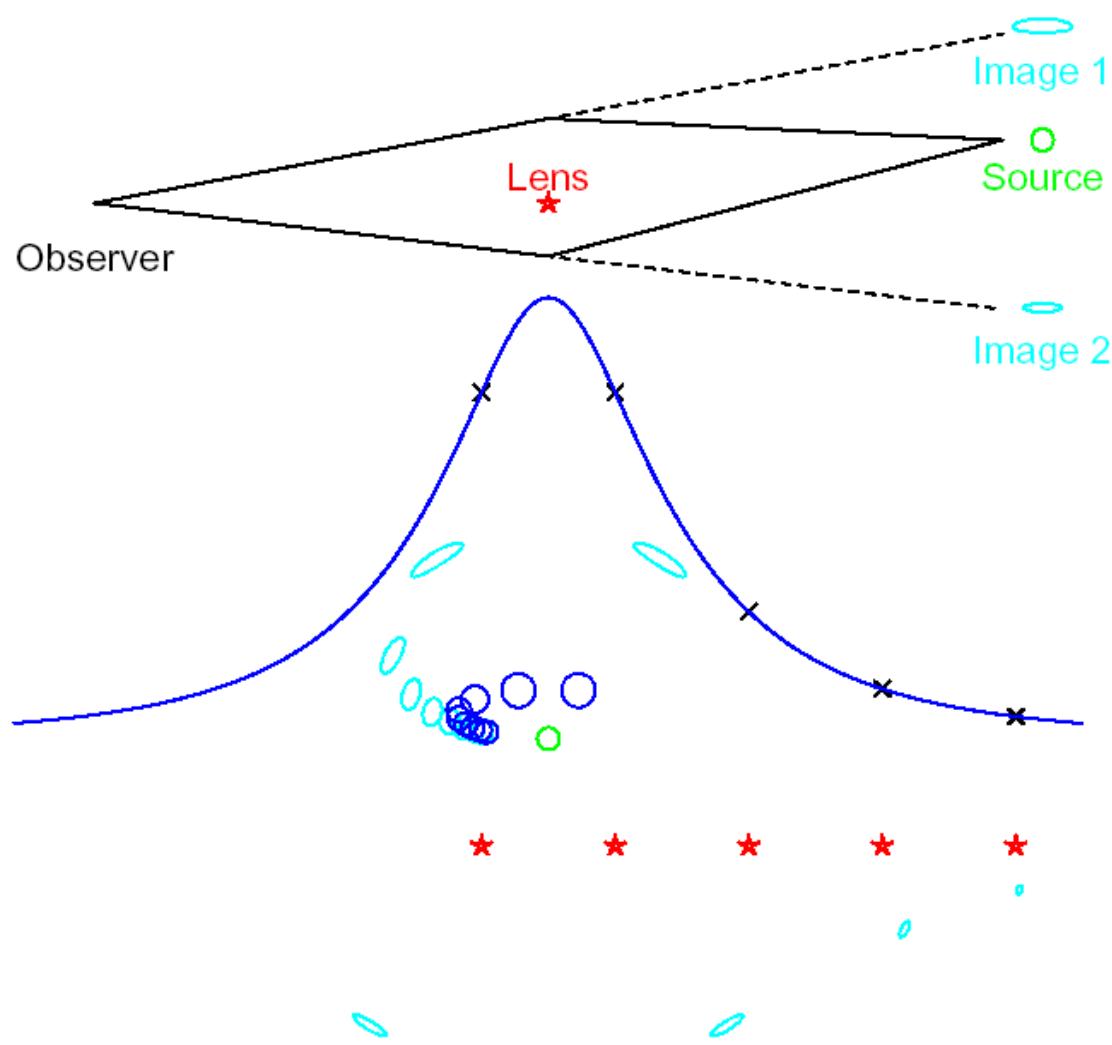
- Bulge G dwarf: 8 mmag
- $\Delta\chi^2 = 100$  requires:  $p_{\text{transit}} = 0.0025/(\delta/0.008)$
- Jupiters:  $a < 160 R_{\text{sun}}$ ;  $P < 250$  days
- Neptunes:  $a < 25 R_{\text{sun}}$ ;  $P < 15$  days
- Earths: (not feasible at bulge)

# Non- $\mu$ lens WFIRST Science: BH + NS in Wide Orbits

- BH+star (5+1) -> 500  $\mu$ as orbit at P = 5 yr
  - ==> 50  $\sigma$  detection for 120,000,000 stars
  - ==> 17  $\sigma$  at P=1 yr
- NS+star (1.4+1) -> 270  $\mu$ as orbit at P = 5 yr
  - ==> 27  $\sigma$  detection for 120,000,000 stars
  - ==> 9  $\sigma$  at P=1 yr

Non-Planet WFIRST  $\mu$ lens Science:  
Isolated BH Mass & Velocity Functions  
(Gould & Yee 2014 ApJ 784 64)  
[Astrometric Microlensing]

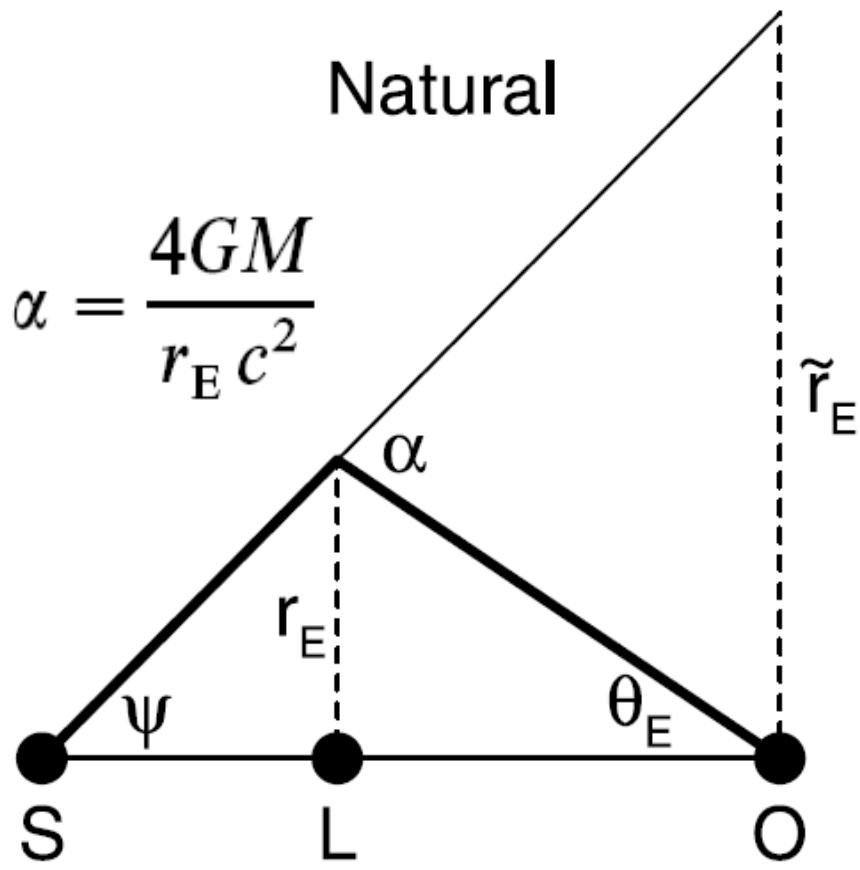
# How Astrometric Microlensing Works



# Non-Planet WFIRST $\mu$ lens Science: Isolated BH Mass & Velocity Functions (Gould & Yee 2014 ApJ 784 64) [Astrometric Microlensing]

- $\Delta\theta = [u/(u^2 + 2)]\theta_E$
- $\theta_E \sim 500 \mu\text{as}$
- $\Delta\theta \sim 150 \mu\text{as}$

# Relation of Mass and Distance to Lensing Observables



$$\alpha = \frac{4GM}{r_E c^2}$$

Natural

$$\alpha/\tilde{r}_E = \theta_E/r_E$$

$$\theta_E \tilde{r}_E = \alpha r_E = \frac{4GM}{c^2}$$

$$\theta_E = \alpha - \psi = \frac{\tilde{r}_E}{D_l} - \frac{\tilde{r}_E}{D_s} = \frac{\tilde{r}_E}{D_{\text{rel}}}$$

$$\tilde{r}_E = \sqrt{\frac{4GMD_{\text{rel}}}{c^2}}$$

$$\theta_E = \sqrt{\frac{4GM}{D_{\text{rel}} c^2}}$$

# Non-Planet WFIRST $\mu$ lens Science: Isolated BH Mass & Velocity Functions (Gould & Yee 2014 ApJ 784 64) [Astrometric Microlensing]

- $\Delta\theta = [u/(u^2 + 2)]\theta_E$
- $\theta_E \sim 500 \mu\text{as}$
- $\Delta\theta \sim 150 \mu\text{as}$

